COMP1730/COMP6730
Programming for Scientists

Sequence types, part 2

Lecture outline

* Lists
* Mutable objects & references

Sequence data types (recap)

* A *sequence* contains $n \geq 0$ values (its *length*), each at an *index* from 0 to $n - 1$.
* python's built-in sequence types:
  - strings (`str`) contain only characters;
  - lists (`list`) can contain a mix of value types;
  - tuples (`tuple`) are like lists, but immutable.
* Sequence types provided by other modules:
  - NumPy arrays (`numpy.ndarray`): all elements in an array must be the same type; typically used for numbers or Boolean values.

Lists

* python's `list` is a general sequence type: elements in a `list` can be values of any type.
* List literals are written in square brackets with comma-separated elements:

```
>>> a_list_of_ints = [2, -4, 2, -8 ]
>>> a_date = [12, "August", 2015]
>>> pairs = [ [ 0.4, True ],
              [ "C", False ] ]
>>> type(pairs)
<class 'list'>
```

Creating lists

```
>>> monday = [18, "July"]
>>> friday = [22, "July"]
>>> [monday, friday]
[ [18, "July"], [22, "July"] ]
>>> list("abcd")
['a', 'b', 'c', 'd']
>>> list(range(10))
[0, 1, 2, 3, 4, 5, 6, 7, 8, 9]
>>> [1/x for x in range(1,6)]
[1.0, 0.5, 0.3333333, 0.25, 0.2]
```

Lists of lists

```
>>> A = [ [1, 2, 3], [4, 5, 6],
          [7, 8, 9] ]
>>> A[0]
[1, 2, 3]
>>> [1, 2, 3][2]
3
>>> A[0][2]
3
```

* Indexing and slicing are *operators*
* Indexing and slicing associate to the left.
  `a_list[i][j] == (a_list[i])[j]`.

Lists of lists

```
>>> A[0]
[1, 2, 3]
>>> A[0:1]
[ [1, 2, 3] ]
>>> A[0:1][1:]
[ ]
>>> A[0:1][1]
IndexError: list index out of range
```

* Indexing a list returns an element, but slicing a list returns a list.

n-dimensional arrays

* NumPy arrays can be *n*-dimensional.

```
>>> np.array([ [1,2,3], [4,5,6] ])
array([[1, 2, 3],
       [4, 5, 6]])
>>> np.zeros( [2, 3] )
array([[ 0., 0., 0.],
       [ 0., 0., 0.]])
>>> np.eye(3)
array([[ 1., 0., 0.]
       [ 0., 1., 0.]
       [ 0., 0., 1.]])
```

* Indexing an n-d array returns an $(n-1)$-d array.

```
>>> A = np.array([[1,2,3],[4,5,6]])
>>> A[0]
array([1,2,3])
>>> np.transpose(A)[0]
array([1,4])
```

* Arrays support extended forms of indexing.

```
>>> A[:,1]
array([2,5])
```

NumPy arrays vs. lists

* Lists can contain an arbitrary *mix* of value types; all values in an array must be of the same type.
* Arrays support more general forms of indexing (*n*-dimensional, indexing with an array of integers or Booleans).
* Arrays support element-wise math operations.
* NumPy/SciPy provides many functions on arrays and matrices (linear algebra, etc).
* Arrays are more (time and memory) efficient, but this matters only when they are large.

Operations on lists

* *list* + *list* concatenates lists:

```
>>> [1, 2] + [3, 4]
[1, 2, 3, 4]
>>> np.array([1, 2]) + np.array([3, 4])
array([4, 6])
```

* *int* * *list* repeats the list:

```
>>> 2 * [1, 2]
[1, 2, 1, 2]
>>> 2 * np.array([1, 2])
array([2, 4])
```

Mutable objects and references

Values are objects

* In python, every value is an *object*.
* Every object has a unique(*) identifier.

```
>>> id(1)
136608064
```

(Essentially, its location in memory.)

* *Immutable* objects never change.
  - For example, numbers (`int` and `float`) and strings.
* *Mutable* objects can change.
  - For example, arrays and lists.

Immutable objects

* Operations on immutable objects create new objects, leaving the original unchanged.

```
>>> a_string = "spam"
>>> id(a_string)
3023147264
>>> b_string = a_string.replace('p', 'l')
>>> b_string
'slam'
>>> id(b_string)
3022616448
>>> a_string
'spam'
```

not the same!

Mutable objects

* A mutable object can be modified yet it's identity remains the same.
* Lists and arrays can be modified through:
  - element and slice assignment; and
  - modifying methods/functions.
* `ndarray` and `list` is the only mutable types we have seen so far but there are many other (sets, dictionaries, user-defined classes).

Element & slice assignment

```
>>> a_list = [1, 2, 3]
>>> id(a_list)
3022622348 ←──────────────────────────────────────────────┐
>>> b_list = a_list                                       │
>>> a_list[2] = 0                                         │
>>> b_list                                                │
[1, 2, 0]                                                 │
>>> b_list[0:2] = ['A', 'B']                              │
>>> a_list                                                │
['A', 'B', 0]                                             │
>>> id(b_list)                                           │
3022622348 ←──────────────────────────────────────────────┘
```

the same object!

Modifying list methods

* `a_list.append(new element)`
* `a_list.insert(index, new element)`
* `a_list.pop(index)`
  - *index* defaults to `-1` (last element).
* `a_list.insert(index, new element)`
* `a_list.extend(an iterable)`
* `a_list.sort()`
* `a_list.reverse()`
* Note: Most do not return a value.

Lists contain references

* Assignment associates a (variable) name with a *reference* to a value (object).
  - The variable still references the same object (unless reassigned) even if the object is modified.
* *A list contains references to its elements.*
* Slicing a list creates a new list, but containing references to the same objects (“shallow copy”).
* Slice assignment *does not copy*.

```
>>> a_list = [1,2,3]
>>> b_list = a_list
>>> a_list.append(4)
>>> print(b_list)
```

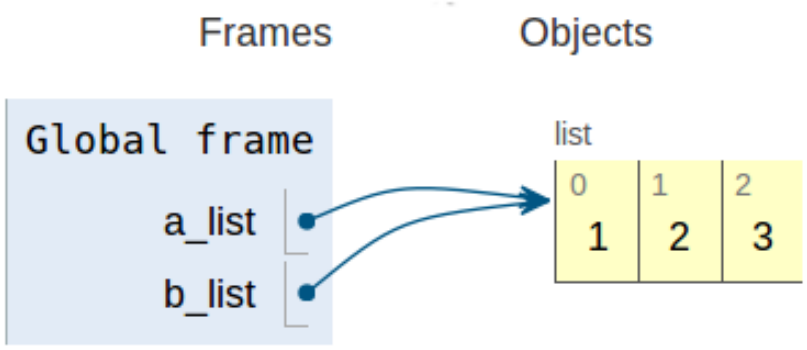

Image from `pythontutor.com`

```
>>> a_list = [1,2,3]
>>> b_list = a_list[:]
>>> a_list.append(4)
>>> print(b_list)
```

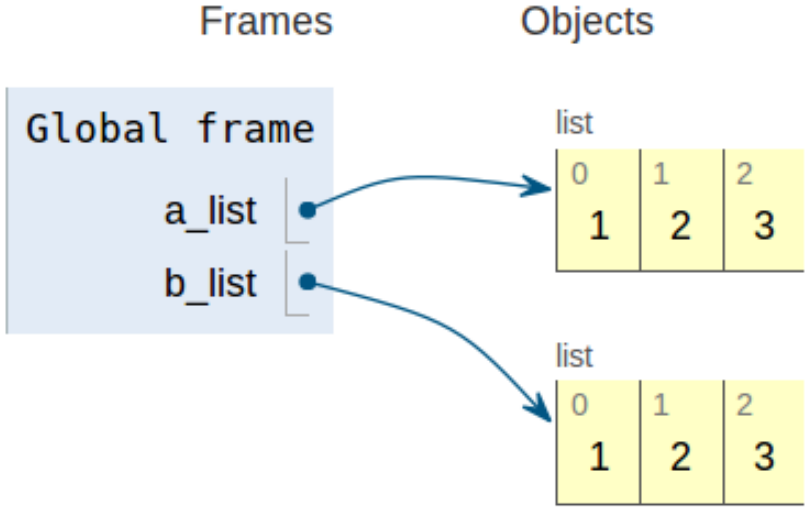

Image from `pythontutor.com`

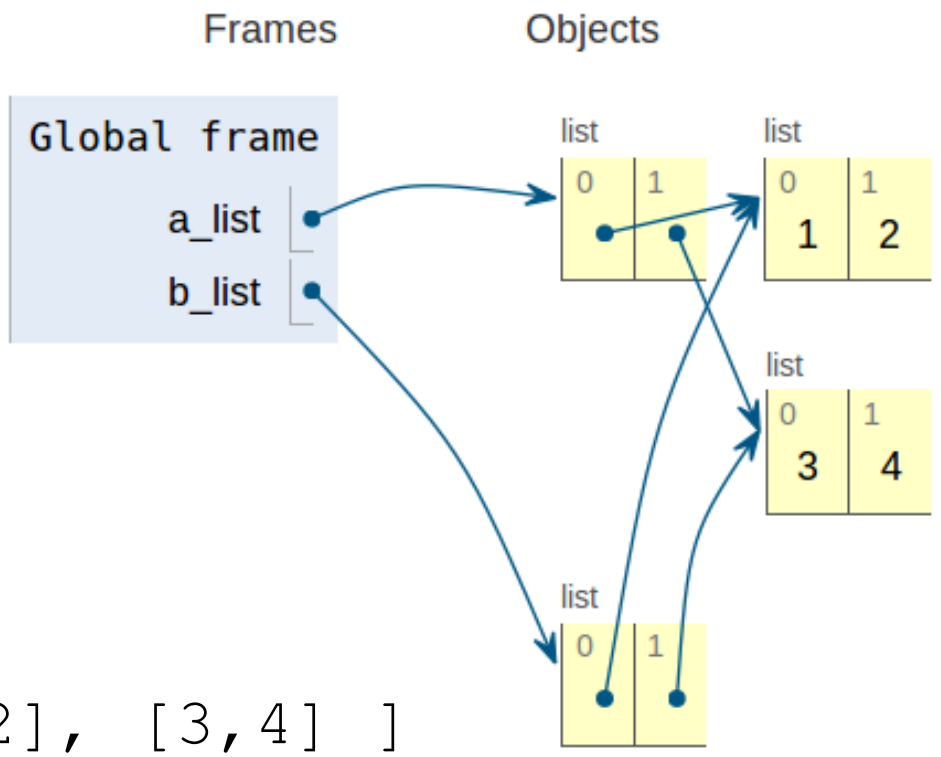

Image from pythontutor.com

```
>>> a_list = [ [1,2], [3,4] ]
>>> b_list = a_list[:]
>>> a_list[0].reverse()
>>> b_list.reverse()
>>> print(b_list)
```

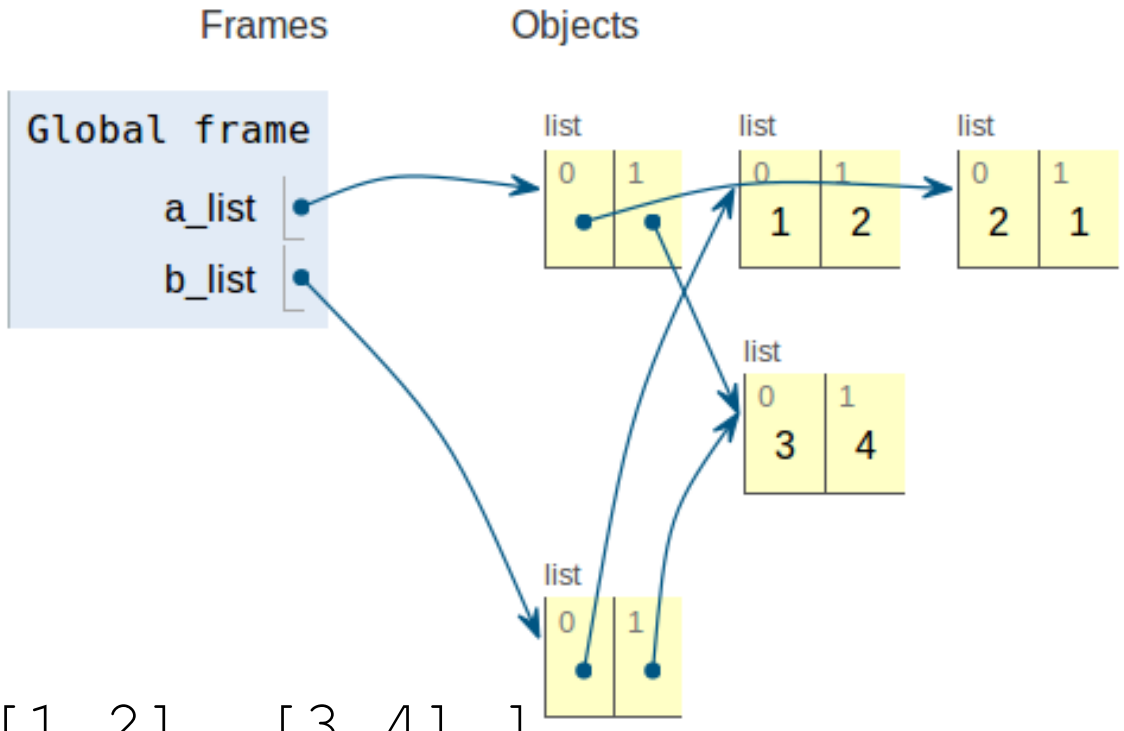

Image from pythontutor.com

```
>>> a_list = [ [1,2], [3,4] ]
>>> b_list = a_list[:]
>>> a_list[0] = a_list[0][::-1]
>>> b_list.reverse()
>>> print(b_list)
```

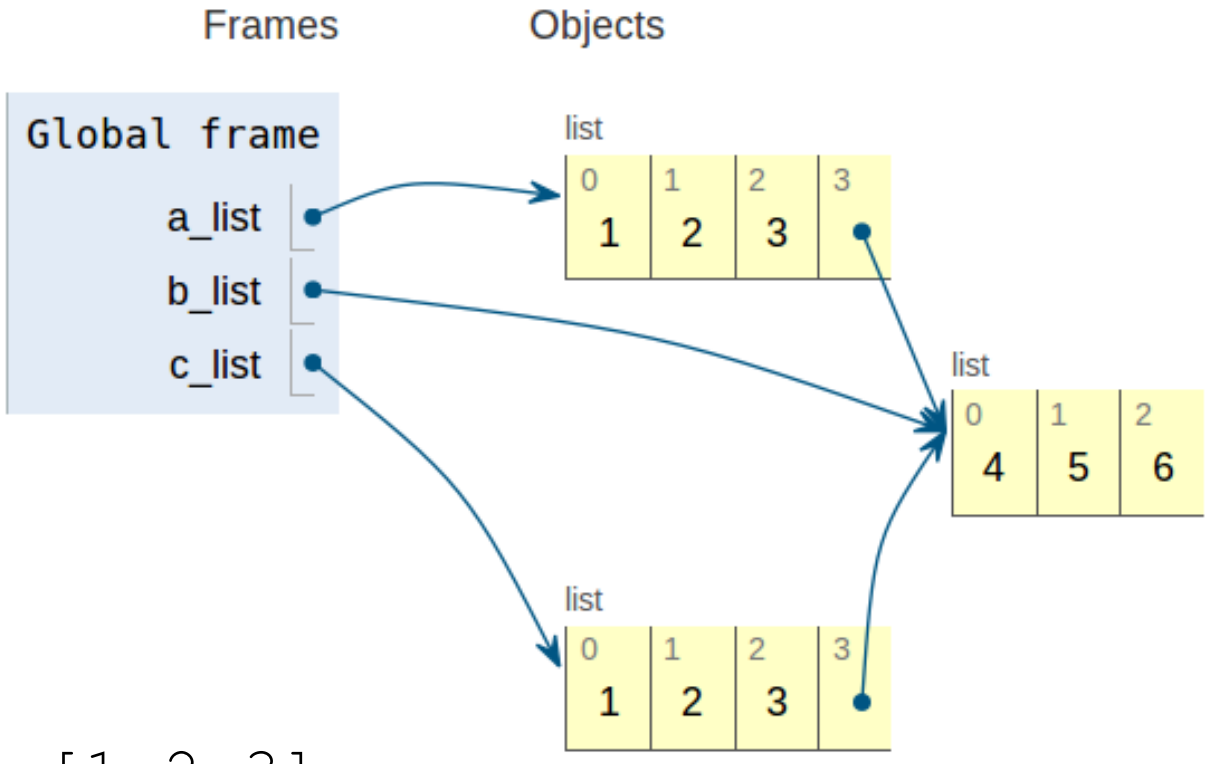

Image from pythontutor.com

```
>>> a_list = [1,2,3]
>>> b_list = [4,5,6]
>>> a_list.append(b_list)
>>> c_list = a_list[:]
>>> b_list[0] = 'A'
```

Common mistakes

```
>>> a_list = [3,1,2]
>>> a_list = a_list.sort()

>>> a_list = [1,2,3]
>>> b_list = a_list
>>> a_list.append(b_list)

>>> a_list = [[]] * 3
>>> a_list[0].append(1)
```

Shallow vs. deep copy

```
>>> import copy
>>> a_list = [[1,2], [3,4]]
>>> id(a_list)
3054870700
>>> id(a_list[0]), id(a_list[1])
(3054874028,3073291596)
>>> b_list = a_list[:]
>>> id(b_list)
3072077420
>>> id(b_list[0]), id(b_list[1])
(3054874028,3073291596)
>>> c_list = copy.deepcopy(a_list)
>>> id(c_list[0]), id(c_list[1])
(3057394764,3057585932)
```

equal!

not equal!

Never use `deepcopy`!

* Creating 10,000 copies of a list of 1,000 lists of 10 integers.

	Time	Memory
Shallow copy	0.4s	39.3 MB
Deep copy	305 s	1071 MB

NumPy arrays

* Slicing arrays does *not (even shallow) copy*:

```
>>> x = np.arange(1,6)
>>> y = x[1:-1]
>>> y
array([2, 3, 4])
>>> x[0:3] = np.zeros(3)
>>> y
array([0, 0, 4])
```

* The slice acts like a “window” into the array.
* Indexing with an array *does* copy.