

COMP1730/COMP6730 Programming for Scientists

Functions, part 2



Announcements

- Homework
 - Homework 4 (submitted yesterday) will be checked in this week lab.
 - Homework 5 is due next Monday (30-Sep-2019).



Lecture outline

- * Recap of functions.
- * Namespaces & references.
- * Recursion revisted.

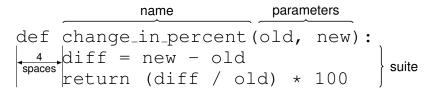


Functions (recap)

- * A *function* is a piece of code that can be *called* by its name.
- * Why use functions?
 - Abstraction: To use a function, we only need to know *what* it does, *not how*.
 - Readability.
 - Divide and conquer break a complex problem into simpler problems.
 - A function is a logical unit of testing.
 - Reuse: Write once, use many times (and by many).



Function definition



- * The function suite is defined by indentation.
- Function *parameters* are variables local to the function suite; their values are set when the function is called.
- The def statement only *defines* the function
 it does not execute the function.



Function call

* To call a function, write its name followed by its arguments in parentheses:

change_in_percent(485, 523)

- Order of evaluation: The argument expressions are evaluated left-to-right, and their values are assigned to the parameters; then the function suite is executed.
- return *expression* causes the function call to end, and return the value of the expression.



Functions without return

- * A function call is an expression: its value is the value return'd by the function.
- In python, functions always return a value: If execution reaches the end of a function suite without executing a return statement, the return value is the special value None of type NoneType.
- Note: None-values are not printed in the interactive shell (unless explicitly with print).



Namespaces



Namespaces

- Assignment associates a (variable) name with a reference to a value.
 - This association is stored in a *namespace* (sometimes also called a "*frame*").
- * Whenever a function is called, a new *local namespace* is created.
- Assignments to variables (including parameters) during execution of the function are done in the local namespace.
- The local namespace disappears when the function call ends.



Scope

- The scope of a variable is "the set of program statements over which a variable exists (i.e., can be referred to)".
 - In other words, the set of program statements over which the namespace that the variable is defined in persists.
- Because there are several namespaces, there can be different variables with the same name in different scopes.



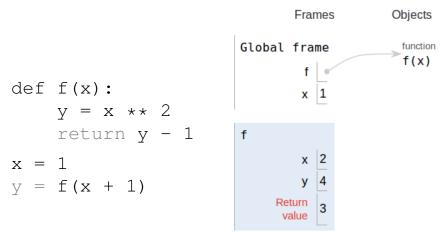


Image from pythontutor.com



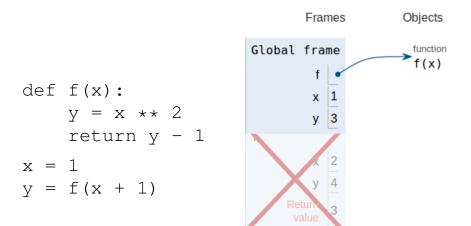


Image based on pythontutor.com



The local assignment rule

- python considers a variable that is assigned anywhere in the function suite to be a "*local* variable" (this includes parameters).
- When a non-local variable is evaluated, its value is taken from the (enclosing) global namespace.
- ★ When a local variable is evaluated, only the local namespace is checked.
 - If the variable is not defined there, python raises an UnboundLocalError.
- * The rule considers only variable assignment.



def f(x):
 return x ** y
>>> y = 2
>>> f(2)
4

def f(x): if y < 1: y = 1return x ** y >>> y = 2>>> f(2) UnboundLocalError: local variable 'y' referenced before assignment



Modifying is not assignment!

- Assignment changes/creates the association between a name and a reference (in the current namespace).
- A modifying operation on a mutable object including index and slice assignment – does not change any name–value association.



def f(x): y = x * * 2f_list.append([x,y]) return y >>> f_list = [] >>> f(2) 4 >>> f(3) 9 >>> f_list [[2, 4], [3, 9]]



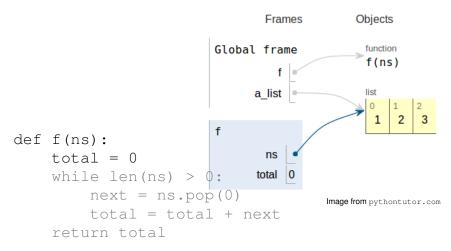
Argument values are references

- When a function is called, its parameters are assigned *references* to the argument values.
 - If an argument value refers to a mutable object (for example, a list), modifications to this object made in the function are visible outside the function's scope.



```
def f(ns):
    total = 0
    while len(ns) > 0:
         next = ns.pop(0)
         total = total + next
    return total
>>> a_{1}ist = [1, 2, 3]
>>> f(a_list)
6
>>> a list
[]
```





>>> a_list = [1,2,3] >>> l_sum = f(a_list)



Other namespaces

- python's built-in functions are defined in a separate namespace; it is searched last if a (non-local) name is not found elsewhere.
- Imported modules are executed in their own namespace.
 - Names in a module namespace are accessed by prefixing the name of the module.
- User-defined classes and objects (not covered in this course) also have their own namespace



Guidelines for good functions

- * Within a function, access only local variables.
 - Use parameters for all inputs to the function.
 - Return all function outputs (for multiple outputs, return a tuple or list).
 - ...except if the specific purpose of the function is to send output elsewhere (e.g., print).
- Don't modify mutable argument values, unless the *specific purpose* of the function is to do that.
- * Rule #4: No rule should be followed off a cliff.



Recursion



- A recursive function is often described as "a function that calls itself".
- ★ Function calls form a *stack*: when the *i*th function call ends, execution returns to where the call was made in the (*i* − 1)th function suite.
- The function suite must have a branching statement, such that a recursive call does not always take place ("base case"); otherwise, recursion never ends.
- Recursion is a way to think about how to solve problems: reducing it to a smaller instance of itself.



Example (contrived)

```
def f(x):
    "Returns 2 ** x.
    x is an integer \geq 0.
    , , ,
    if x == 0:
        return 1
                        # base case
    else:
        y = f(x - 1) # recursive call
        return 2 * y
```



. . .

1 def f(x):

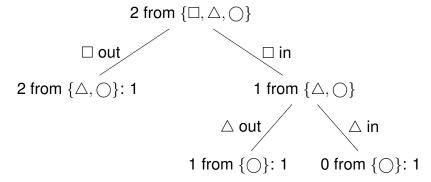
2 y =
$$f(2)$$

x = 2
3 if x == 0:
4 else:
5 y = $f(x - 1)$
x = 1
6 if x == 0:
7 else:
8 y = $f(x - 1)$
y if x == 0:
10 return 1
x = 1, y = 1
11 return 2 * y
x = 2, y = 2
12 return 2 * y



Example: Counting selections

 Compute the number of ways to choose a subset of k elements from a set of n, C(n, k).





* Recursive formulation:

$$C(n,k) = C(n-1,k) + C(n-1,k-1)$$

 $C(n,0) = 1$
 $C(n,n) = 1$

```
def choices(n, k):
    if k == n or k == 0:
        return 1
    else:
        return choices(n - 1, k) + \
            choices(n - 1, k - 1)
```





4 choices(n - 1, k) n = 2, k = 2 5 if k == 0 or k == n: 6 return 1 7 choices (n - 1, k - 1)n = 2, k = 1 8 if k == 0 or k == n: 9 else: 10 <u>choices(n - 1, k)</u> n = 1, k = 1 11 if k == 0 or k == n: 12 return 1 13 choices (n - 1, k - 1) n = 1, k = 0 14 if k == 0 or k == n: 15 return 1 16 return 1 + 1 17 return 1 + 2

ans = 3



Example: Sudoku

