

COMP1730/COMP6730 Programming for Scientists

Functions, part 2



Lecture outline

- * Recap of functions
- * Namespaces & references
- * Recursion revisted

Functions (recap)

- * A *function* is a piece of code that can be *called* by its name.
- * Why use functions?
 - Abstraction: To use a function, we only need to know what it does, not how.
 - Readability.
 - Divide and conquer break a complex problem into simpler problems.
 - A function is a logical unit of testing.
 - Reuse: Write once, use many times (and by many).

Function definition

- ★ The function suite is defined by indentation.
- * Function *parameters* are variables local to the function suite; their values are set when the function is called.
- The def statement only defines the function
 it does not execute the function.

Function call

* To call a function, write its name followed by its arguments in parentheses:

```
change_in_percent (485, 523)
```

- * Order of evaluation: The argument expressions are evaluated left-to-right, and their values are assigned to the parameters; then the function suite is executed.
- * return expression causes the function call to end, and return the value of the expression.



Functions without return

- * A function call is an expression: its value is the value return'd by the function.
- * In python, functions always return a value: If execution reaches the end of a function suite without executing a return statement, the return value is the special value None of type NoneType.
- Note: None-values are not printed in the interactive shell (unless explicitly with print).



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Namespaces

- Assignment associates a (variable) name with a reference to a value.
 - This association is stored in a namespace (sometimes also called a "frame").
- * Whenever a function is called, a new *local* namespace is created.
- Assignments to variables (including parameters) during execution of the function are done in the local namespace.
- The local namespace disappears when the function call ends.

Scope

- * The *scope* of a variable is "the set of program statements over which a variable exists (i.e., can be referred to)".
 - In other words, the set of program statements over which the namespace that the variable is defined in persists.
- * Because there are several namespaces, there can be different variables with the same name in different scopes.

def f(x):

$$y = x ** 2$$

return $y - 1$
 $x = 1$
 $y = f(x + 1)$

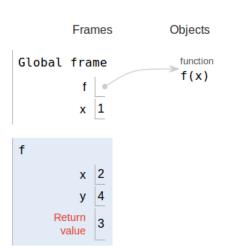


Image from pythontutor.com



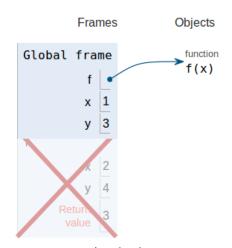


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The local assignment rule

- python considers a variable that is assigned anywhere in the function suite to be a "local variable" (this includes parameters).
- * When a non-local variable is evaluated, its value is taken from the (enclosing) global namespace.
- * When a local variable is evaluated, only the local namespace is checked.
 - If the variable is not defined there, python raises an UnboundLocalError.
- * The rule considers only *variable assignment*.

```
def f(x):
                    def f(x):
    return x ** v
                         if y < 1:
                             v = 1
>>> y = 2
                         return x ** y
>>> f(2)
                    >>> y = 2
                    >>> f(2)
                    UnboundLocalError:
                     local variable 'y'
                     referenced before
                     assignment
```



- * Modifying is not assignment!
 - Assignment changes/creates the association between a name and a reference (in the current namespace).
 - A modifying operation on a mutable object including index and slice assignment – does not change any name–value association.

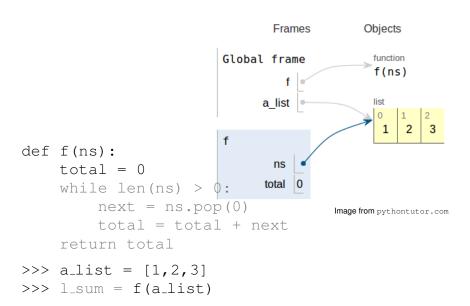
```
def f(x):
    y = x ** 2
    f_list.append([x,y])
    return y
>>> f_list = []
>>> f(2)
>>> f(3)
>>> f_list
[[2, 4], [3, 9]]
```



Argument values are references

- * When a function is called, its parameters are assigned *references* to the argument values.
 - If an argument value refers to a mutable object (for example, a list), modifications to this object made in the function are visible outside the function's scope.

```
def f(ns):
    total = 0
    while len(ns) > 0:
        next = ns.pop(0)
        total = total + next
    return total
>>> a_list = [1,2,3]
>>> f(a_list)
6
>>> a_list
```





Other namespaces

- python's built-in functions are defined in a separate namespace; it is searched last if a (non-local) name is not found elsewhere.
- Imported modules are executed in their own namespace.
 - Names in a module namespace are accessed by prefixing the name of the module.
- User-defined classes and objects (not covered in this course) also have their own namespace

Guidelines for good functions

- * Within a function, access only local variables.
 - Use parameters for all inputs to the function.
 - Return all function outputs (for multiple outputs, return a tuple or list).
 - ...except if the specific purpose of the function is to send output elsewhere (e.g., print).
- ⋆ Don't modify mutable argument values, unless the *specific purpose* of the function is to do that.
- * Rule #4: No rule should be followed off a cliff.



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- * A recursive function is often described as "a function that calls itself".
- ★ Function calls form a *stack*: when the *i*th function call ends, execution returns to where the call was made in the (*i* − 1)th function suite.
- * The function suite must have a branching statement, such that a recursive call does not always take place ("base case"); otherwise, recursion never ends.
- Recursion is a way to think about how to solve problems: reducing it to a smaller instance of itself.

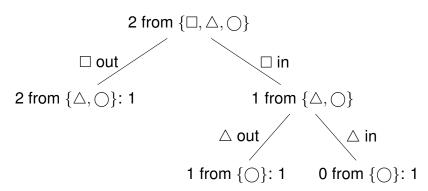
Example (contrived)

```
def f(x):
    '''Returns 2 ** x.
    x is an integer >= 0.
    , , ,
    if x == 0:
                        # hase case
        return 1
    else:
        y = f(x - 1) # recursive call
        return 2 * v
```

```
1 def f(x):
2 y = f(2)
                  x = 2
               3 \text{ if } x == 0:
               4 else:
               5 y = \underline{f(x - 1)}
                                      x = 1
                                   6 if x == 0:
                                   7 else:
                                   8 y = f(x - 1)
                                                      9 if x == 0:
                                                      10 return 1
                                     x = 1, y = 1
                                  11 return 2 * y
                  x = 2, y = 2
               12 return 2 * y
```

Example: Counting selections

* Compute the number of ways to choose a subset of k elements from a set of n, C(n, k).



* Recursive formulation:

def choices(n, k):

$$C(n, k) = C(n-1, k) + C(n-1, k-1)$$

 $C(n, 0) = 1$
 $C(n, n) = 1$

```
1 \text{ ans} = \text{choices}(3,2)
```

```
n = 3, k = 2
2 if k == 0 or k == n:
3 else:
4 choices (n - 1, k)
                n = 2, k = 2
              5 if k == 0 or k == n:
              6 return 1
7 choices(n-1, k-1)
                n = 2, k = 1
              8 if k == 0 or k == n:
              9 else:
             10 choices (n - 1, k)
                              n = 1, k = 1
                           11 if k == 0 or k == n:
                           12 return 1
             13 choices (n - 1, k - 1)
                              n = 1, k = 0
                           14 if k == 0 or k == n:
```

```
4 choices (n - 1, k)
                 n = 2, k = 2
               5 \text{ if } k == 0 \text{ or } k == n:
               6 return 1
7 choices (n - 1, k - 1)
                 n = 2, k = 1
              8 if k == 0 or k == n:
              9 else:
              10 <u>choices(n - 1, k)</u>
                                 n = 1, k = 1
                             11 if k == 0 or k == n:
                             12 return 1
              13 choices (n - 1, k - 1)
                                n = 1, k = 0
                             14 if k == 0 or k == n:
                             15 return 1
              16 return 1 + 1
17 return 1 + 2
```

ans = 3



Example: Sudoku

