COMP1730/COMP6730
Programming for Scientists

Functions

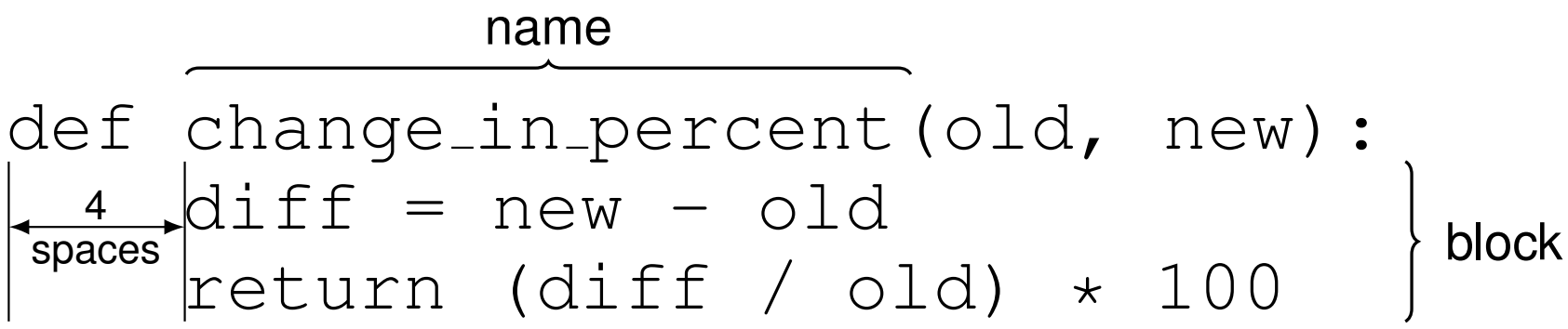
Lecture outline

* Function definition.
* Function calls & order of evaluation.
* Assignments in functions; local variables.
* Function testing & documentation.

Functions

* In programming, a *function* is a piece of the program that is given a name, and can be *called* by that name.
* Functions definitions promote *abstraction* (“what, not how”) and help break a complex problem into smaller parts.
* To encapsulate computations on data, functions have *parameters* and a *return value*.

Function definition (reminder)



* A function definition consists of a name and body (a block).
* The extent of the block is defined by indentation, which must be the same for all statements of a block (standard is 4 spaces).

Function definition

parameters

```
def change_in_percent(old, new):
    diff = new - old
    return (diff / old) * 100
```

* Function (formal) *parameters* are (variable) names; they can be used only in the function body.
* Parameters' values will be set only when the function is called.
* `return` is a statement: when executed, it causes the function call to end, and return the value of the expression

Function call

* To call a function, write its name followed by its (actual) *arguments* in parentheses:

```
>>> change_in_percent(489, 556)
13.701431492842536
```

* The arguments are expressions.
* Their number should match the parameters.
  - Some exceptions; more about this later.
* A function call is an expression: its value is the value returned by the function (which may be None).

Function Call Execution

Order of evaluation

* The python interpreter always executes instructions one at a time in sequence; this includes expression evaluation.
* To evaluate a function call, the interpreter:
  - First, evaluates the argument expressions, one at a time, from left to right.
  - Then, executes the function suite with its parameters assigned the values returned by the argument expressions.
* Same with operators: first arguments (left to right), then the operation.

The call stack

* When evaluation of a function call begins, the current instruction sequence is put “on hold” while the expression is evaluated.
* When execution of the function ends, the interpreter returns to the next instruction after where the function was called.
* The “to-do list” of where to come back to after each current function call is called the (execution or call) *stack*.

```
import math

# Convert degrees to radians.
def deg_to_rad(x):
    return x * math.pi / 180

# Take sin of an angle in degrees.
def sin_of_deg(x):
    x_in_rad = deg_to_rad(x)
    return math.sin(x_in_rad)

ans = sin_of_deg(23)
print(ans)
```

```
1  import math
2  def deg_to_rad(x):
       ...
3  def sin_of_deg(x):
       ...
4  ans=sin_of_deg(23)
                          5  x_in_rad=deg_to_rad(23)
                                                    6  return 23*math.pi/180
                          7  x_in_rad=0.4014
                          8  return math.sin(0.4014)
9  ans = 0.3907
10 print(ans)
```

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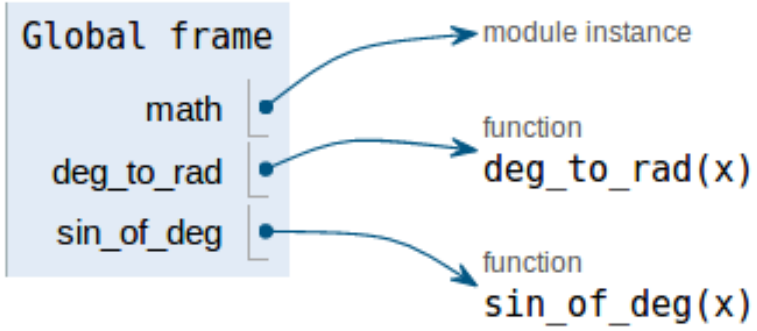
import math

def deg_to_rad(x):
    return x * math.pi / 180

def sin_of_deg(x):
    x_in_rad = deg_to_rad(x)
    return math.sin(x_in_rad)

answer = sin_of_deg(23)
```



(Image from pythontutor.com)

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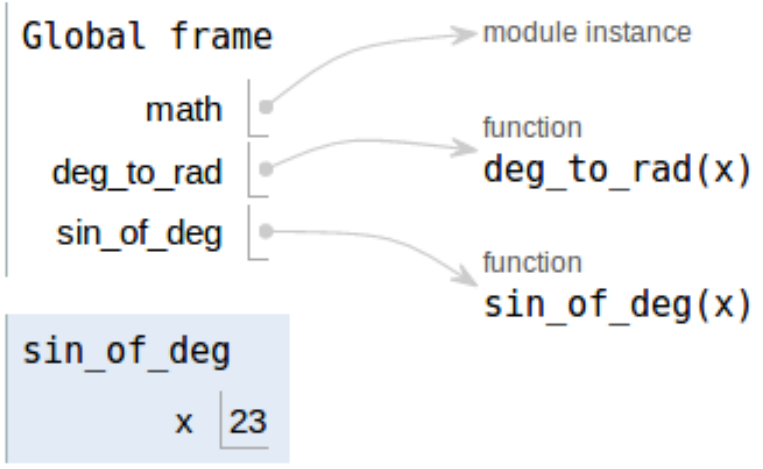

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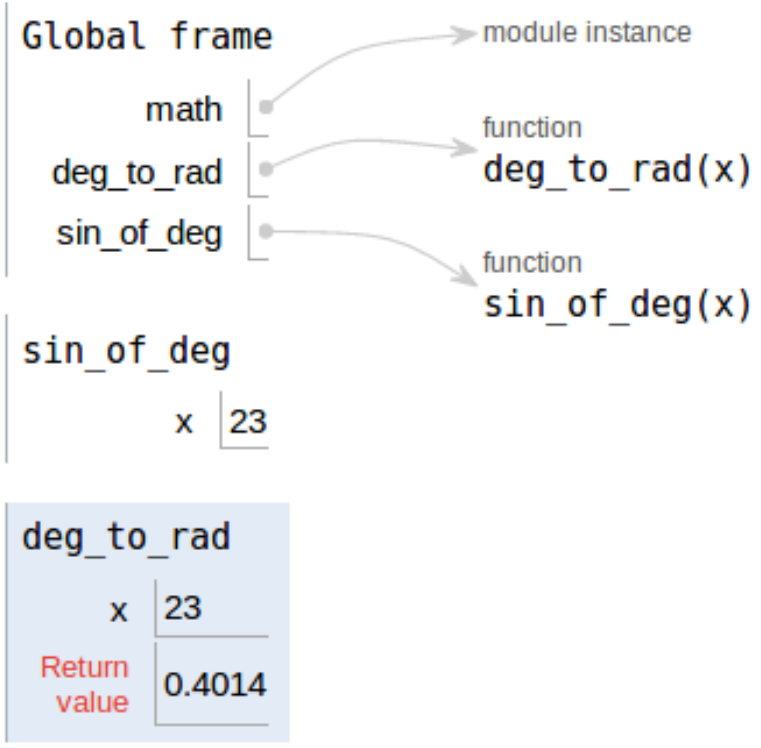

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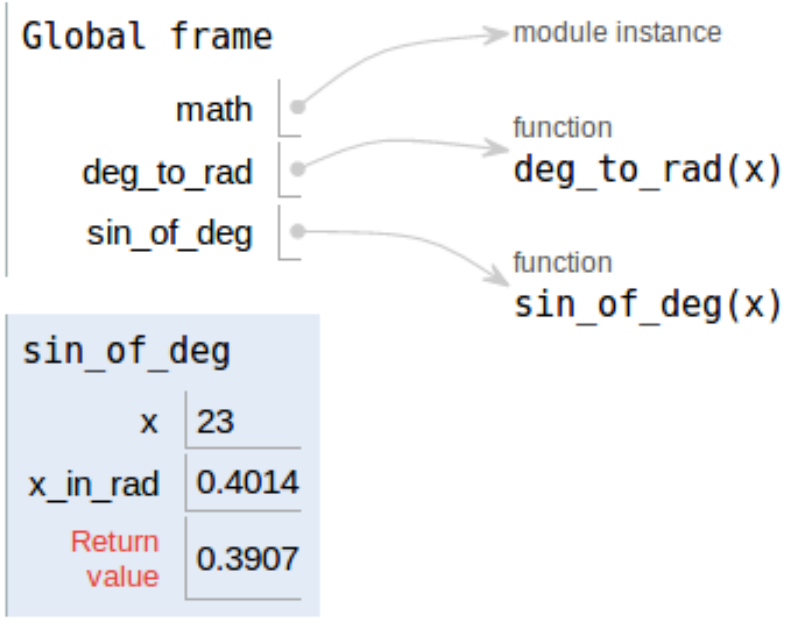

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def sin_of_deg(x):
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answer = sin_of_deg(23)
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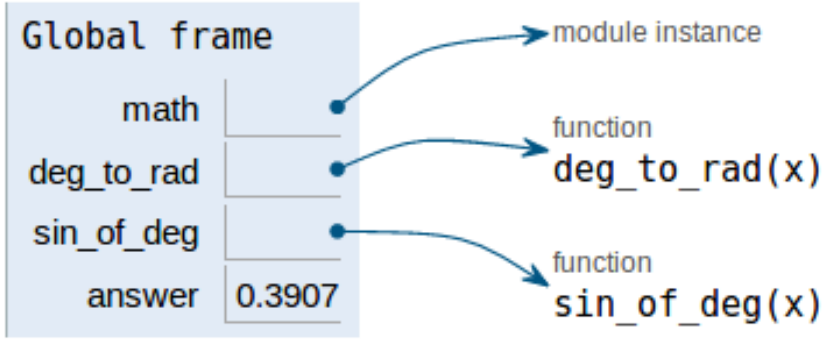


(Image from `pythontutor.com`)

Assignments in functions

* Variables assigned in a function (including parameters) are *local* to the function.
  - Local variables are have scope limited to the enclosing block – the interpreter uses a new namespace for each function call.
  - Local variables that are not parameters are undefined before the first assignment in the function body.
  - Variables with the same name used outside the function are unchanged after the call.
* The full story is a little more complicated – we'll return to it later in the course.

Functions with no `return`

* If execution of a function reaches the end of the body without encountering a `return` statement, the function call returns the special value `None`.
  - `None` is used to indicate "no value".
  - The type of `None` is `NoneType` (different from any other value).
* In interactive mode, the interpreter does *not* print the return value of an expression when the value is `None`.

Side effects and return values

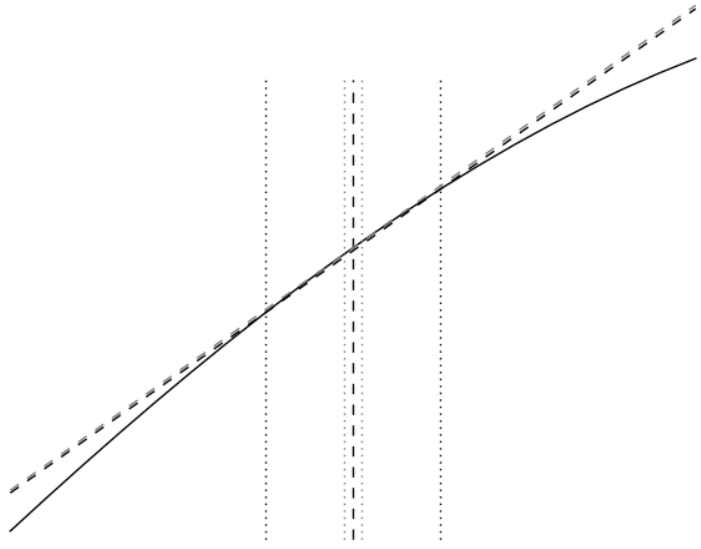
* An expression *evaluates to* a value.
* A statement does not return a value, but executing it causes something to happen, e.g.,
  - `a_number = 2 + 3` : variable `a_number` becomes associated with the value `5`;
  - `print(2 + 3)` : the value `5` is printed.

  This is called a *side effect*.
* We can write functions with or without side effects, and functions that do or don't return a value (other than `None`).

* Functions with side effects and `None` return:
  - `robot.drive_right()`
  - `print(...)`
* Functions with return value and no side effect:
  - `math.sin(x)`
  - `change_in_percent(old, new)`
* Functions with side effects and return value?
  - Possible.
* Functions with no side effect and `None` return value?

Functions of functions

* In python, functions are also values: a function can be passed as argument to another function.
* Example: Compute an approximation of the derivative of any function at a point.



```
def derivative(f, x, d):
    return (f(x + d) - f(x - d)) / (2*d)

ans = derivative(math.sin, math.pi/4, 0.1)
```

Testing and Documentation

Function testing

* A function is a logical unit of testing.
  - Document the assumptions (for example, type and range of argument values);
  - Test a variety of cases under the assumptions.
* What are “edge cases”?
  - Typical (numeric) examples: values equal to/less than/greater than zero; very large and very small values; values of equal and opposite signs; etc.
* Remember that floating-point numbers have limited precision; == can fail.

```
>>> change_in_percent(1, 2)
100.0
>>> change_in_percent(2, 1)
-50.0
>>> change_in_percent(1, 1)
0.0
>>> change_in_percent(1, -1)
-200.0
>>> change_in_percent(0, 1)
ZeroDivisionError
```

The function docstring

```
def change_in_percent(old, new):
    '''Return change from old to new, as
    a percentage of the old value.
    old value must be non-zero.'''
    return ((new - old) / old) * 100
```

* A *docstring* is a string literal written as the first statement inside a function's body.
* Acts like a comment, but accessible through the built-in help system.
* Describe *what* the function does (if not obvious from its name), and its *limits* and *assumptions*.