

COMP 3610/6361

(re-recording of 02/08/23)

06/08/2023

- Ed Stem
- Quiz (Voluntary)
- Assessment 1
- Course Representative

successor (next step in a computation):

$$\langle E, s \rangle \rightarrow \langle E', s' \rangle$$

- chaining is possible

$$\langle E, s \rangle \rightarrow \langle E', s' \rangle \rightarrow \langle E'', s'' \rangle \dots$$

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Derivation tree of one single computation step

$$\frac{\frac{\vdots}{a' \rightarrow b'} \quad \frac{\vdots}{c' \rightarrow d'}}{a \rightarrow \zeta} \text{ rules}$$

provides a proof  
that the successor  
is reachable.

$\langle 42, !l, \emptyset \rangle$  does not have a successor,  
we say  $\langle 42 + !l, \emptyset \rangle$  is stuck.

$\langle !l, \emptyset \rangle \not\rightarrow$  we can't find a  
successor

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op<sup>2</sup>

$\langle 42 + !l, \emptyset \rangle \rightarrow \not\rightarrow$

↑  
the empty function /  
empty storage/store

no location has been assigned a value.

Slide 43

$$s + \{l_2 \mapsto 0\} = s$$

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$$\langle l_2 := 0, s \rangle \longrightarrow \langle \text{skip}, s + \{l_2 \mapsto 0\} \rangle \quad \text{assign 1}$$

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$$\langle E, s \rangle \longrightarrow \langle \text{skip}; \text{while } !l_1 \geq 1 \text{ do } \dots, s + \{l_2 \mapsto 0\} \rangle \quad \text{seq 2}$$

$$E = l_2 := 0; \text{while } !l_1 \geq 1 \text{ do } (l_2 := !l_2 + !l_1; l_1 := !l_1 + -1)$$

$$s = \{l_1 \mapsto ?, l_2 \mapsto 0\}$$

$\langle \text{skip}; \text{while } !l_1 \geq 1 \text{ do } (\dots), s \rangle$

$\rightarrow \langle \text{while } !l_1 \geq 1 \text{ do } \dots, s \rangle$

$\rightarrow \langle \text{if } !l_1 \geq 1 \text{ then "body"; while } (!l_1 \geq 1) \dots \text{ else skip}, s \rangle$

$\rightarrow \langle \text{if } 3 \geq 1 \text{ then "body"; while } \dots \text{ else skip}, s \rangle$

$\rightarrow \dots$

$E = l_2 := 0; \text{while } !l_1 \geq 1 \text{ do } \underbrace{(l_2 := !l_2 + !l_1; l_1 := !l_1 + -1)}_{\text{"body"}}$

$s = \{ l_1 \mapsto 3, l_2 \mapsto 0 \}$

$$\langle \ell := 1; 0 \rangle + \langle \ell := 2; 0 \rangle, \{\ell \mapsto 0\} \rangle$$

$$\rightarrow \langle \text{skip}; 0 + \langle \ell := 2; 0 \rangle, \{\ell \mapsto 1\} \rangle$$

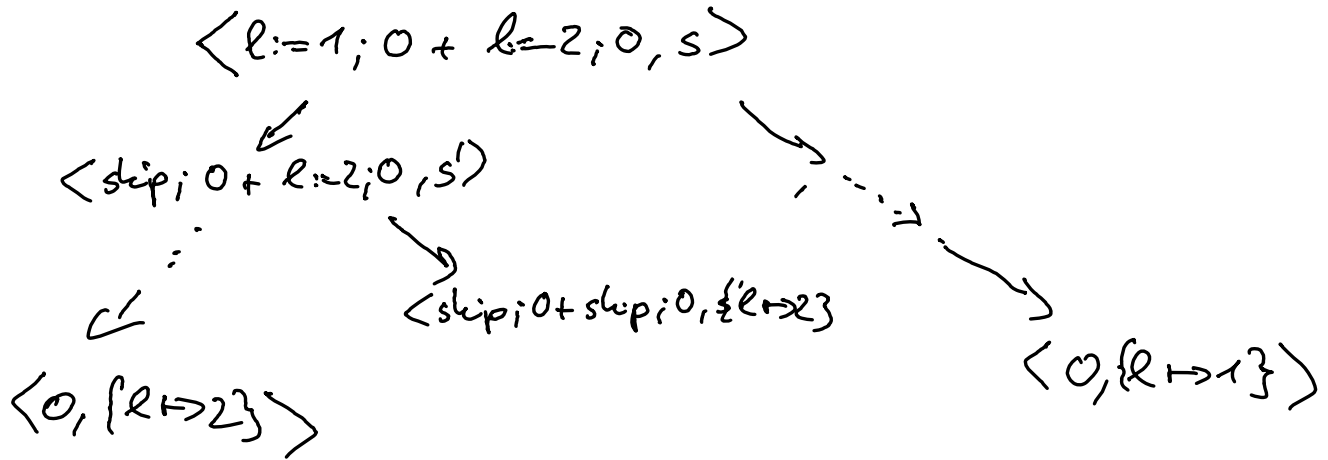
$$\rightarrow \langle 0 + \langle \ell := 2; 0 \rangle, \{\ell \mapsto 1\} \rangle$$

$$\rightarrow \langle 0 + \langle \text{skip}; 0 \rangle, \{\ell \mapsto 2\} \rangle$$

$$\rightarrow \langle 0 + 0, \{\ell \mapsto 2\} \rangle$$

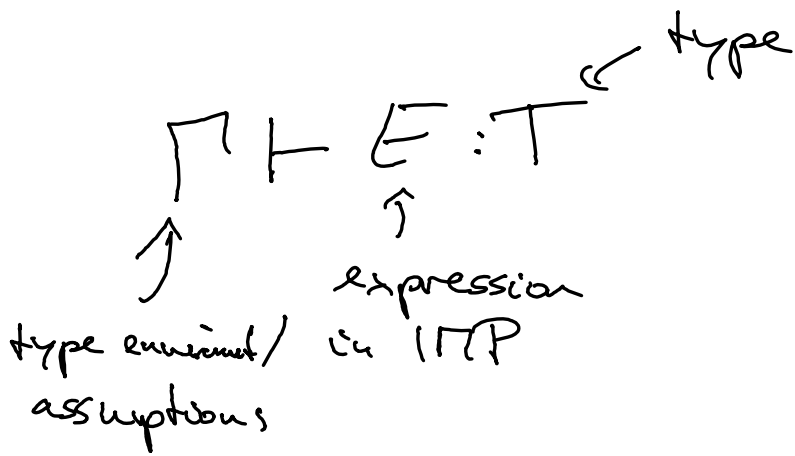
$$\rightarrow \langle 0, \{\ell \mapsto 2\} \rangle$$

$NP$  (incl  $OP1$  and  $OP2$ ) +  $OP1' + OP2'$



non-deterministic  
language





$E$  is of type  $T$  if the assumptions in  $\Gamma$  are satisfied.

$\{\} \vdash \text{false} : \text{bool}$		$\{\} \vdash 2 : \text{int}$		$\{\} \vdash 3 : \text{int}$		$\{\} \vdash 4 : \text{int}$
$\{\} \vdash \text{if false then 2 else 3+4} : \text{int}$			$\{\} \vdash 3+4 : \text{int}$	$\text{opt}$		

if