

Comp 3610/6361

03/08/2023

$\Gamma \vdash E : T$

↑ ↑ ↙ type

 expression/program

type environment/
assumptions

E is of type T if assumptions in Γ
are satisfied.

$$\text{dom}(\Gamma) \subseteq \text{dom}(s)$$

Γ
 type environment

s
 state/store

Example

$$\Gamma = \{ l \mapsto \text{intref}, m \mapsto \text{intref} \}$$

$$\Gamma: \mathcal{L} \rightarrow \text{Type}$$

$$\text{dom}(\Gamma) = \{l, m\}$$

$$\Gamma(x) = \begin{cases} \text{intref} & \text{if } x = l \\ \text{intref} & \text{if } x = m \\ \text{undefined} & \text{otherwise} \end{cases}$$

Example

$$s = \{l \mapsto 3, m \mapsto 5, o \mapsto 27\}$$

s is partial function of type

$$\mathbb{L} \rightarrow \text{Int}$$

$$s(x) = \begin{cases} 3 & \text{if } x = l \\ 5 & \text{if } x = m \\ 27 & \text{if } x = o \\ \text{undefined} & \text{or} \end{cases}$$

$$\text{dom}(s) = \{l, m, o\}$$

$$\{ \text{essent} \} \overset{E}{\underbrace{m := !l + 2 : \text{unit}}}$$

\uparrow
given value

$\langle E, \{ l \mapsto 3, m \mapsto 7 \} \rangle \rightarrow \dots$
guaranteed by
progress

$\langle E, \emptyset \rangle \not\rightarrow$

Type Checking

$\{l \mapsto \text{intref}\} \vdash !l \geq 3 : \text{bool}$

$\frac{\frac{\checkmark}{\Pi(l) = \text{intref}} \quad \frac{\quad}{\{l \mapsto \text{intref}\} \vdash !l+1 : \text{int}}}{\{l \mapsto \text{intref}\} \vdash l := !l+1 : \text{unit}}$

$\{l \mapsto \text{intref}\} \vdash \text{while } !l \geq 3 \text{ do } l := !l+1 : \text{unit}$

Syntax of IMP

$E ::= n \mid b \mid \text{skip} \mid$

$E \text{ op } E \mid E ; E \mid$

$\text{if } E \text{ then } E \text{ else } E \mid$

Base (s) show property for n, b, skip

QCF