

COMP 3610/6361

31/08/2023

Small-step  $\vee$  big-step

equivalence

$\langle c, s \rangle \Rightarrow s'$

$\Downarrow$  to show

$\langle c, s \rangle \rightarrow^* \langle \text{Skip}, s' \rangle$

is this enough.

What about  
 $E := l_1 := 0;$   
while true do  
 $l_1 := !l_1 + 1$

$\langle E, s \rangle \not\rightarrow ?$

- no final state in big-step semantics
- no final state in small-step either;  
but infinite sequence

$$\langle c, s \rangle \xrightarrow[\text{skip}]{*} \langle \text{skip}, s' \rangle$$

$\Leftrightarrow$

$$\langle c, s \rangle \xrightarrow[\text{skip}]{*} \langle \text{skip}, s' \rangle$$

$\uparrow$        $\uparrow$   
 con       $\text{skip}$

$$\langle !l := 3+4, s \rangle \xrightarrow[\text{skip}]{*} \langle !l := 7, s \rangle \rightarrow \langle \text{skip}, s' \rangle$$

$\downarrow$

$$\langle !l := 3+4, s \rangle \xrightarrow[\text{skip}]{*} \langle \text{skip}, s' \rangle$$

$$\langle l := 1, s \rangle \rightarrow \langle \text{skip}, s(l \mapsto 1) \rangle \quad \checkmark \text{ true}$$

$$\langle l := 1, s \rangle \rightarrow \langle l := 2, s \rangle \quad \times \text{ false}$$

$$f: \text{int} * \text{int} \Rightarrow \text{int}$$

$$f: (x, y) = x + y$$

$$f(3, 4) = 7$$

$$f \ 3$$

$$f: \text{int} \Rightarrow (\text{int} \Rightarrow \text{int})$$

$$f: x \ y = x + y$$

$$f \ 3 \ 4 = 7$$

$$f \ 3 = 3 + y$$

