

COMP4011/8011 Advanced Topics in Formal Methods and Programming Languages

– Software Verification with Isabelle/HOL –

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Section 18

[AutoCorres and C Verification](#page-1-0)

wp

apply (wp *extra wp rules*)

Tactic for automatic application of **weakest precondition rules**

- originally developed by Thomas Sewell, NICTA
- knows about a huge collection of existing wp rules for monads
- works best when precondition is a schematic variable
- related tool: **wpc** for Hoare reasoning over **case** statements

When used with **AutoCorres**, allows automated reasoning about C programs.

This Chapter: AutoCorres and C verification.

[Demo – Introduction to AutoCorres and wp](#page-3-0)

[A Brief Overview of C and Simpl](#page-4-0)

C

Main new problems in verifying C programs:

- expressions with side effects
- more control flow (do/while, for, break, continue, return)
- local variables and blocks
- functions & procedures
- concrete C data types
- C memory model and C pointers

C is not a nice language for reasoning. Things are going to get ugly. AutoCorres will help.

C Parser: translates C into Simpl

Simpl: deeply embedded imperative language in Isabelle.

- generic imperative language by Norbert Schirmer, TU Munich
- state space and basic expressions/statements can be instantiated
- has operational semantics
- has its own Hoare logic with soundness and completeness proof, plus automated vcg
- **C Parser:** parses C, produces Simpl definitions in Isabelle
	- written by Michael Norrish, NICTA and ANU
	- Handles a non-trivial subset of C
	- Originally written to verify seL4's C implementation
	- AutoCorres is built on top of the C Parser

Commands in Simpl

```
datatype ('s, 'p, 'f) com =
      Skip
    | Basic "'s \Rightarrow 's"
    | Spec "('s * 's) set"
    | Seq "('s, 'p, 'f) com" "('s, 'p, 'f) com"
    | Cond "'s set" "('s, 'p, 'f) com" "('s, 'p, 'f) com"
    | While "'s set" "('s, 'p, 'f) com"
    | Call 'p
    | DynCom "'s \Rightarrow ('s, 'p, 'f) com"
    | Guard 'f "'s set" "('s, 'p, 'f) com"
    | Throw
    | Catch "('s, 'p, 'f) com" "('s, 'p, 'f) com"
```
's = state, **'p** = procedure names, **'f** = faults

Expressions with side effects

 $a = a * b; x = f(h); i = ++i - i++; x = f(h) + g(x);$

- \cdot **a** = \mathbf{a} \star **b** \sim Fine: easy to translate into Isabelle
- **x = f(h)** Fine: may have side effects, but can be translated sanely.
- **i = ++i i++** Seriously? What does that even mean? Make this an error, force programmer to write instead: $i0 = i$; $i + i$; $i = i - i0$; (or just $i = 1$)
- $x = f(h) + g(x)$ Ok if **g** and **h** do not have any side effects \implies Prove all functions in expressions are side-effect free

Alternative:

Explicitly model nondeterministic order of execution in expressions.

Control flow

do { c } **while** (condition);

automatically translates into:

c: **while** (condition) { c }

Similarly:

for (init; condition; increment) { c }

becomes

init; **while** (condition) { c; increment; }

More control flow: break/continue

```
while ( condition ) {
   foo ;
   if (Q) continue;
   bar ;
   if (P) break;
}
```
Non-local control flow: **continue** goes to condition, **break** goes to end. Can be modelled with exceptions:

- throw exception **'continue'**, catch at end of body.
- throw exception **'break'**, catch after loop.

Break/continue

Break/continue example becomes:

```
t r y {
    while ( condition ) {
        t r y {
             foo ;
             if (Q) { exception = 'continue'; throw; }
             bar ;
             if (P) { exception = 'break'; throw; }
        } catch { i f ( exception == ' continue ') SKIP else throw; }
    }
} catch { i f ( exception == ' break ') SKIP else throw; }
```
This is not C any more. But it models C behaviour!

Need to be careful that only the translation has access to exception state.

Return

```
if (P) return x;
foo ;
return y ;
```
Similar non-local control flow. **Similar solution:** use throw/try/catch

```
t r y {
    if (P) { return_val = x; exception = 'return'; throw;}
    foo ;
    return_val = y; exception = 'return'; throw;
} catch {
    SKIP
}
```


[AutoCorres](#page-13-0)

AutoCorres

AutoCorres: reduces the pain in reasoning about C code

- Written by David Greenaway, NICTA and UNSW
- Converts C/Simpl into (monadic) shallow embedding in Isabelle
- Shallow embedding easier to reason about than Simpl

Is self-certifying: produces Isabelle theorems proving its own correctness

For each Simpl definition C and its generated shallow embedding A:

- AutoCorres proves an Isabelle theorem stating that C refines A
- Every behaviour of C has a corresponding behaviour of A
- Refinement guarantees that properties proved about A will also hold for C.
- (Provided that A never fails. c.f. Total Correctness)

AutoCorres Process

L1: initial monadic shallow embedding

- **L2:** local variables introduced by λ-bindings
- **HL:** heap state abstracted into a set of typed heaps

WA: machine words abstracted to idealised integers or nats

Output: human-readable output with type strengthening, polish

On-the-fly proof:

Simpl refines **L1** refines **L2** refines **HL** refines **WA** refines **Output**

Example: C99

We will use the following example program to illustrate each of the phases.

```
unsigned some_func(unsigned *a, unsigned *b, unsigned c) {
  unsigned * p = NULL;
```

```
if (c > 10u)p = a;
 } else {
   p = b:
  }
  return *p;
}
```


Example: Simpl

```
some_func_body ≡
TRY
  \pi :== ptr_coerce (Ptr (scast 0));;
  I F 0 xA < ´c THEN
     ´p :== ´a
  ELSE
    \tau \bar{p} : == \tau \bar{b}F I ;;
  Guard C_Guard {c_guard p}
   ( creturn global_exn_var_ ' _update ret__unsigned_ ' _update
      (\lambda s. h_val (hrs_mean (t_hrs)' (globals s))) (p' s));;
  Guard DontReach {} SKIP
CATCH SKIP END
```


Example: L1 (monadic shallow embedding)

```
11 some_func \equiv L1 seq (L1 init ret__unsigned_' _update)
 (L1 seq (L1 modify (p_ ' _update (λ_. ptr_coerce ( Ptr ( scast 0)))))
   (L1 seq (L1 condition (\lambdas. 0xA < c_' s)
                            (L1 modify (\lambda s. s \ln' : = a' s)(L1 modify (\lambda s. s(p_-' := b_ ' s))(L1 seq (L1 guard (λs. c_guard (p_ ' s )))
        (L1 seq (L1_modify (\lambdas. s(|ret_unsigned ' :=
                 h_val ( hrs_mem ( t_hrs ' ( globals s ))) (p_' s)\binom{n}{2}(L1 modify (global exn var ' update (\lambda. Return )))))))
```
State type is the same as Simpl, namely a record with fields:

- **globals**: heap and type information
- **a '**, **b '**, **c '**, **p '** (parameters and local variables)
- **ret unsigned '**, **global exn var '** (return value, exception type)

Example: L2 (local variables lifted)

```
12 some func a b c \equivL2 seq (L2 lcondition (\lambdas. 0 xA < c)
                        (L2_qets (\lambda s. a) [''p'']( L2 gets (λs. b) [''p ' ']))
  (λp. L2 seq (L2 guard (λs. c_guard p ))
     (λ_. L2 gets (λs. h_val ( hrs_mem ( t_hrs_ ' s )) p) ['' ret ' ']))
```
State is a record with just the **globals** field

- function now takes its parameters as arguments
- local variable **p** now passed via λ -binding
- **L2 gets** annotated with local variable names
- This ensures preservation by later AutoCorres phases

Example: HL (heap abstracted into typed heaps)

```
hl_some_func a b c \equivL2 seq (L2 lcondition (\lambdas. 0 xA < c)
                          (L2_qets (\lambda s. a) [''p''](L2_qets (\lambda s. b) [''p''](λr . L2 seq (L2 guard (λs . is_valid_w32 s r ))
    (\lambda_{-}. L2_gets (\lambda_{s}. heap_w32 s r) [''ret'']))
```
State is a record with a set of **is valid** and **heap** fields:

- These store **pointer validity** and **heap contents** respectively, per type
- above example has only 32-bit word pointers

Heap Abstraction

 C Memory Model AutoCorres Typed Heaps

C Memory Model: by Harvey Tuch

- **Heap** is a mapping from 32-bit addresses to bytes: 32 word ⇒ 8 word
- **Heap Type Description** stores type information for each heap location

Example: WA (words abstracted to ints and nats)

```
wa some func a b c \equivL2 seq (L2 condition (\lambdas. 10 < c)
                             (L2_qets (\lambda s. a) [''p''](L2_qets (\lambda s. b) [''p''](\lambda r. \text{ L2-seq } (L2 quard (\lambda s. \text{ is valid}, w32 s r))(\lambda_{-}. L2_gets (\lambda_{s}. unat (heap_w32 s r)) [''ret'']))
```
Word abstraction: C **int** → Isabelle int, C **unsigned** → Isabelle nat

- Guards inserted to ensure absence of unsigned underflow and overflow
- Signed under/overflow already has guards (it has undefined behaviour)

In the example, the **unsigned** argument **c** is now of type **nat**

- The function also returns a nat result
- The heap is not abstracted, hence the call to **unat**

Example: Output (type strengthening and polish)

```
some func' a b c \equivDO p \leftarrow oreturn (if 10 < c then a else b);
    oquard (\lambda s. is_{\text{valid\_w32}} s);
    ogets (\lambda s. unat (heap_w32 s p))OD
```
Type Strengthening:

- Tries to convert output to a more restricted monad
- The above is in the **option** monad because it doesn't modify the state, but might fail
- The **type** of the option monad implies it cannot modify state

Polish:

- Simplify output as much as possible
- The **condition** has been rewritten to a **return** because the condition **10** < **c** doesn't depend on the state

Type Strengthening

Example:

unsigned zero (void){ return 0u; }

Effect information now encoded in function **types Later proofs get this information for free!** Can be controlled by the **ts force** option of AutoCorres

(Reader) Option Monad

Another standard monad, familiar from e.g. Haskell

Return:

$$
\\
$$
 $x \equiv \lambda s$. Some x

Bind:

obind *a b* ≡ λ*s*. case *a s* of None ⇒ None | Some *r* ⇒ *b r s*

- Infix notation: $|\gg$
- Do notation: DO ... OD

ovalid (*P x*) (oreturn *x*) *P*

Hoare Logic:

ovalid *P f Q* ≡ ∀ *s r*. *P s* ∧ *f s* = Some *r* −→ *Q r s*

V *r*. ovalid (*R r*) (*g r*) *Q* ovalid *P f R* ovalid $P(f \gg q) Q$

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Exception Monad

Exceptions used to model early return, break and continue.

Exception Monad: $\mathbf{\hat{s}} \Rightarrow ((\mathbf{\hat{e}} + \mathbf{\hat{a}}) \times \mathbf{\hat{s}})$ set \times bool

- Instance of the nondeterministic state monad: return-value type is **sum type** *'e* + *'a*
- Sum Type Constructors: **Inl** :: $'e \Rightarrow 'e + 'a$ **Inr** :: $'a \Rightarrow 'e + 'a$
- Convention: Inl used for exceptions, Inr used for ordinary return-values

Basic Monadic Operations

returnOk
$$
x \equiv
$$
 return (lnr x) throwError $e \equiv$ return (lnl e)
lift $b \equiv (\lambda x \cdot \text{case } x \text{ of } \text{ln} \mid e \Rightarrow \text{throwError } e \mid \text{ln} \mid r \Rightarrow b \mid r)$
bindE: $a \gg=E b \equiv a \gg=(\text{lift } b)$ Do notation: doE ... odE

Hoare Rules for Exceptions

New kind of Hoare triples to model normal and exceptional cases:

$$
\{P\} f \{Q\}, \{E\}
$$

=

$$
\{P\} f \{\lambda x \text{ s. case } x \text{ of } \text{ln} \mid e \Rightarrow E \text{ es } | \text{ ln} \mid r \Rightarrow Q \mid r \text{ s } \}
$$

Weakest Precondition Rules:

 $\{P \mid P \mid x\}$ returnOk $x \{P\}, \{E\}$ $\{E \mid e\}$ throwError $e \{P\}, \{E\}$ \bigwedge x. $\{R \; x\} \; b \; x \; \{Q\}, \{E\} \quad \{P\} \; a \; \{R\}, \{E\}$ $\{P\}$ *a* \gg = E *b* $\{Q\}$, $\{E\}$ (other rules analogous)

We have seen

- The automated proof method **wp**
- The C Parser and translating C into Simpl
- AutoCorres and translating Simpl into monadic form
- The option and exception monads