

# COMP4011/8011 Advanced Topics in Formal Methods and Programming Languages

## Software Verification with Isabelle/HOL –

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## Section 18

## AutoCorres and C Verification



wp

apply (wp extra\_wp\_rules)

Tactic for automatic application of weakest precondition rules

- originally developed by Thomas Sewell, NICTA
- knows about a huge collection of existing wp rules for monads
- works best when precondition is a schematic variable
- related tool: wpc for Hoare reasoning over case statements

When used with AutoCorres, allows automated reasoning about C programs.

This Chapter: AutoCorres and C verification.

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# Demo - Introduction to AutoCorres and wp

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# A Brief Overview of C and Simpl



C

#### Main new problems in verifying C programs:

- · expressions with side effects
- more control flow (do/while, for, break, continue, return)
- local variables and blocks
- functions & procedures
- concrete C data types
- · C memory model and C pointers

C is not a nice language for reasoning.

Things are going to get ugly.

AutoCorres will help.



# C Parser: translates C into Simpl

Simpl: deeply embedded imperative language in Isabelle.

- generic imperative language by Norbert Schirmer, TU Munich
- state space and basic expressions/statements can be instantiated
- has operational semantics
- has its own Hoare logic with soundness and completeness proof, plus automated vcg
- C Parser: parses C, produces Simpl definitions in Isabelle
  - written by Michael Norrish, NICTA and ANU
  - Handles a non-trivial subset of C
  - Originally written to verify seL4's C implementation
  - AutoCorres is built on top of the C Parser

## Commands in Simpl

```
datatype ('s, 'p, 'f) com =
      Skip
    | Basic "'s \Rightarrow 's"
    | Spec "('s * 's) set"
    | Seq "('s, 'p, 'f) com" "('s, 'p, 'f) com"
    | Cond "'s set" "('s, 'p, 'f) com" "('s, 'p, 'f) com"
    | While "'s set" "('s, 'p, 'f) com"
    | Call 'p
    | DynCom "'s \Rightarrow ('s, 'p, 'f) com"
    | Guard 'f "'s set" "('s, 'p, 'f) com"
    I Throw
    | Catch "('s, 'p, 'f) com" "('s, 'p, 'f) com"
```

's = state, 'p = procedure names, 'f = faults

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# Expressions with side effects

```
a = a * b; x = f(h); i = ++i - i++; x = f(h) + g(x);
```

- **a = a \* b** Fine: easy to translate into Isabelle
- **x** = **f(h)** Fine: may have side effects, but can be translated sanely.
- i = ++i i++ Seriously? What does that even mean? Make this an error, force programmer to write instead:
  - i0 = i; i++; i = i i0; (or just i = 1)
- x = f(h) + g(x) Ok if g and h do not have any side effects
   Prove all functions in expressions are side-effect free

#### Alternative:

Explicitly model nondeterministic order of execution in expressions.



## Control flow



## More control flow: break/continue

```
while (condition) {
   foo;
   if (Q) continue;
   bar;
   if (P) break;
}
```

Non-local control flow: **continue** goes to condition, **break** goes to end. Can be modelled with exceptions:

- throw exception 'continue', catch at end of body.
- throw exception 'break', catch after loop.



### Break/continue

Break/continue example becomes:

```
try {
    while (condition) {
        try {
            foo;
            if (Q) { exception = 'continue'; throw; }
            bar;
            if (P) { exception = 'break'; throw; }
        } catch { if (exception == 'continue') SKIP else throw; }
}
catch { if (exception == 'break') SKIP else throw; }
```

#### This is not C any more. But it models C behaviour!

Need to be careful that only the translation has access to exception state.



## Return

```
if (P) return x;
foo;
return y;
```

Similar non-local control flow. Similar solution: use throw/try/catch

```
try {
    if (P) { return_val = x; exception = 'return'; throw; }
    foo;
    return_val = y; exception = 'return'; throw;
} catch {
    SKIP
}
```



## **AutoCorres**



## **AutoCorres**

AutoCorres: reduces the pain in reasoning about C code

- Written by David Greenaway, NICTA and UNSW
- Converts C/Simpl into (monadic) shallow embedding in Isabelle
- Shallow embedding easier to reason about than Simpl

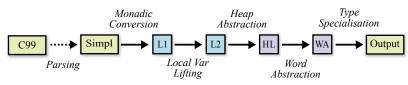
**Is self-certifying:** produces Isabelle theorems proving its own correctness

For each Simpl definition *C* and its generated shallow embedding *A*:

- AutoCorres proves an Isabelle theorem stating that C refines A
- Every behaviour of C has a corresponding behaviour of A
- Refinement guarantees that properties proved about A will also hold for C.
- (Provided that A never fails. c.f. Total Correctness)



## **AutoCorres Process**



L1: initial monadic shallow embedding

**L2:** local variables introduced by  $\lambda$ -bindings

HL: heap state abstracted into a set of typed heaps

WA: machine words abstracted to idealised integers or nats

Output: human-readable output with type strengthening, polish

#### On-the-fly proof:

Simpl refines L1 refines L2 refines HL refines WA refines Output

## Example: C99

We will use the following example program to illustrate each of the phases.

```
unsigned some_func(unsigned *a, unsigned *b, unsigned c) {
  unsigned *p = NULL;

if (c > 10u){
   p = a;
} else {
   p = b;
}

return *p;
}
```



## Example: Simpl

```
some_func_body =
TRY
  p :== ptr_coerce (Ptr (scast 0));;
  IF 0xA < c THEN
    'p :== 'a
  ELSE
    'p :== 'b
  F1;;
  Guard C_Guard {c_guard 'p}
   (creturn global_exn_var_', update ret_unsigned_', update
     (\lambda s. h_val (hrs_mem (t_hrs_' (globals s))) (p_' s)));;
  Guard DontReach {} SKIP
CATCH SKIP END
```

# Example: L1 (monadic shallow embedding)

State type is the same as Simpl, namely a record with fields:

- globals: heap and type information
- a\_', b\_', c\_', p\_' (parameters and local variables)
- ret\_unsigned\_', global\_exn\_var\_' (return value, exception type)



# Example: L2 (local variables lifted)

```
\label{eq:local-condition} \begin{split} \text{12\_some\_func a b c} &\equiv \\ \text{L2\_seq (L2\_condition } (\lambda s. \ 0 x \text{A} < c) & (\text{L2\_gets } (\lambda s. \ a) \ [''p'']) \\ & (\text{L2\_gets } (\lambda s. \ b) \ [''p''])) \\ & (\lambda p. \ \text{L2\_seq (L2\_guard } (\lambda s. \ c\_guard \ p)) \\ & (\lambda \_. \ \text{L2\_gets } (\lambda s. \ h\_val \ (\text{hrs\_mem } (\text{t\_hrs\_'} \ s)) \ p) \ [''ret''])) \end{split}
```

#### State is a record with just the globals field

- function now takes its parameters as arguments
- local variable **p** now passed via  $\lambda$ -binding
- L2\_gets annotated with local variable names
- This ensures preservation by later AutoCorres phases



# Example: HL (heap abstracted into typed heaps)

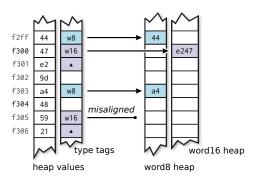
State is a record with a set of is\_valid\_ and heap\_ fields:

- These store pointer validity and heap contents respectively, per type
- above example has only 32-bit word pointers



## Heap Abstraction





#### C Memory Model: by Harvey Tuch

- **Heap** is a mapping from 32-bit addresses to bytes: 32 word ⇒ 8 word
- · Heap Type Description stores type information for each heap location



## Example: WA (words abstracted to ints and nats)

#### Word abstraction: C int $\rightarrow$ Isabelle int, C unsigned $\rightarrow$ Isabelle nat

- Guards inserted to ensure absence of unsigned underflow and overflow
- Signed under/overflow already has guards (it has undefined behaviour)

#### In the example, the **unsigned** argument **c** is now of type **nat**

- The function also returns a nat result.
- The heap is not abstracted, hence the call to unat



## Example: Output (type strengthening and polish)

```
some_func' a b c ≡
DO p ← oreturn (if 10 < c then a else b);
  oguard (λs. is_valid_w32 s p);
  ogets (λs. unat (heap_w32 s p))
OD</pre>
```

#### **Type Strengthening:**

- · Tries to convert output to a more restricted monad
- The above is in the option monad because it doesn't modify the state, but might fail
- The **type** of the option monad implies it cannot modify state

#### Polish:

- · Simplify output as much as possible
- The condition has been rewritten to a return because the condition
   10 < c doesn't depend on the state</li>



# Type Strengthening

#### Example:

```
unsigned zero(void){ return Ou; }
```

<b>Monad Type</b>	Kind	Туре	Example
pure	Pure function	'a	0
gets	Read-only, non-failing	$s \Rightarrow a$	$\lambda$ s. 0
option	Read-only function	$s \Rightarrow a \text{ option}$	oreturn 0

Effect information now encoded in function types

Later proofs get this information for free!

Can be controlled by the ts\_force option of AutoCorres

# (Reader) Option Monad

Another standard monad, familiar from e.g. Haskell

#### Return:

oreturn 
$$x \equiv \lambda s$$
. Some  $x$ 

#### Bind:

obind  $a b \equiv \lambda s$ . case a s of None  $\Rightarrow$  None | Some  $r \Rightarrow b r s$ 

- Infix notation: |>>>
- · Do notation: DO ... OD

#### **Hoare Logic:**

ovalid 
$$P f Q \equiv \forall s r. P s \land f s = Some r \longrightarrow Q r s$$

ovalid 
$$(P x)$$
 (oreturn  $x$ )  $P$  
$$\frac{\bigwedge r. \text{ ovalid } (R r) \ (g r) \ Q \quad \text{ovalid } P f R}{\text{ovalid } P \ (f \mid \gg g) \ Q}$$



# **Exception Monad**

**Exceptions** used to model early return, break and continue.

```
Exception Monad: \dot{s} \Rightarrow ((\dot{e} + \dot{a}) \times \dot{s}) \text{ set } \times \text{ bool }
```

- Instance of the nondeterministic state monad: return-value type is sum type 'e + 'a
- Sum Type Constructors: InI ::  $\dot{e} \Rightarrow \dot{e} + \dot{a}$  Inr ::  $\dot{a} \Rightarrow \dot{e} + \dot{a}$
- Convention: Inl used for exceptions, Inr used for ordinary return-values

#### **Basic Monadic Operations**

```
 \begin{array}{lll} {\sf returnOk} \ x \ \equiv \ {\sf return} \ ({\sf Inr} \ x) & {\sf throwError} \ e \ \equiv \ {\sf return} \ ({\sf Inl} \ e) \\ {\sf lift} \ b \ \equiv \ (\lambda x. \ {\sf case} \ x \ {\sf of} \ {\sf Inl} \ e \ \Rightarrow {\sf throwError} \ e \ | \ {\sf Inr} \ r \ \Rightarrow b \ r) \\ \end{array}
```

**bindE:**  $a \gg = E b \equiv a \gg = (lift b)$  **Do notation:** doE ... odE



## Hoare Rules for Exceptions

New kind of Hoare triples to model normal and exceptional cases:

#### **Weakest Precondition Rules:**



## We have seen

- The automated proof method wp
- The C Parser and translating C into Simpl
- AutoCorres and translating Simpl into monadic form
- The option and exception monads