

Abstract Data Types: Lists 1

A1

ADTs

The List ADT

A List interface and its implementation: Array List

Abstract Data Types (ADTs)

Abstract data types describe the behaviour (semantics) of a data type without specifying its implementation. An ADT is thus abstract, not concrete.

A **container** is a very general ADT, serving as a holder of objects. A **list** is an example of a specific container ADT.

An ADT is described in terms of the semantics of the operations that may be performed over it.

The List ADT

The **list** ADT is a container known mathematically as a *finite sequence* of elements. A list has these fundamental properties:

- duplicates *are* allowed
- order is preserved

A list may support operations such as these:

- *create*: construct an empty list
- *add*: add an element to the list
- *is empty*: test whether the list is empty

Our List Interface

We will explore lists using a simple interface:

```
public interface List<T> {  
    void add(T value);  
    T get(int index);  
    int size();  
    T remove(int index);  
    void reverse();  
}
```

```
void add(T value);
```

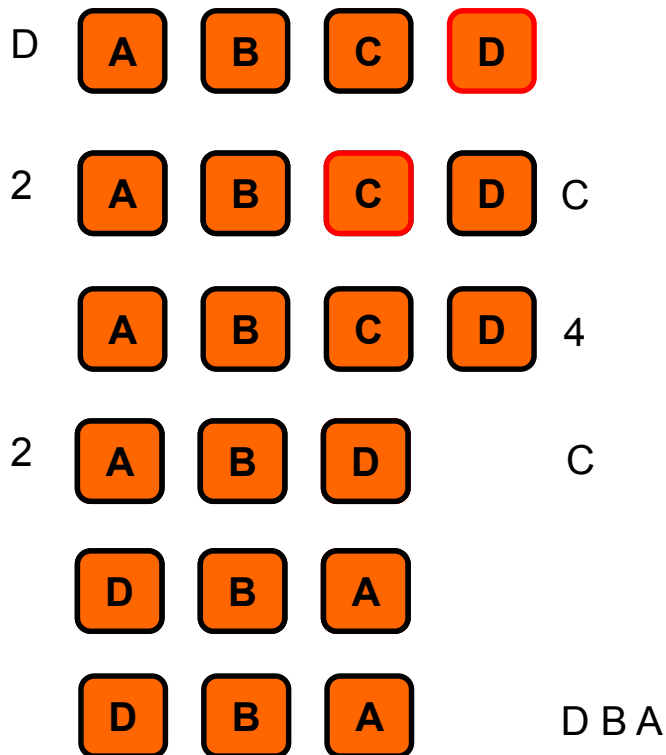
```
T get(int index);
```

```
int size();
```

```
T remove(int index);
```

```
void reverse();
```

```
String toString();
```



List Implementation

- Arrays
 - Fast lookup of any element
 - A little messy to grow and contract
- Linked list
 - Logical fit to a list, easy to grow, contract
 - Need to traverse list to find arbitrary element

Abstract Data Types: Lists 2

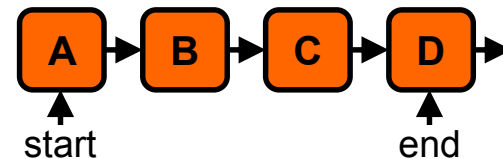
A2

A List interface and its implementation: Linked List

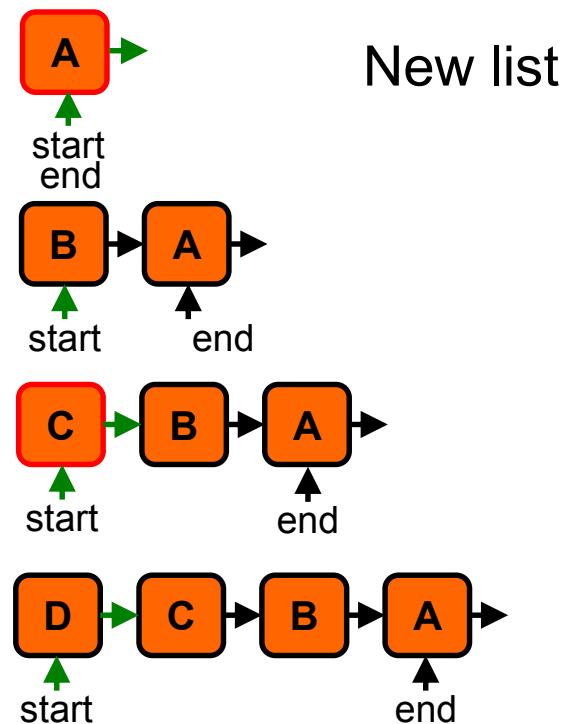
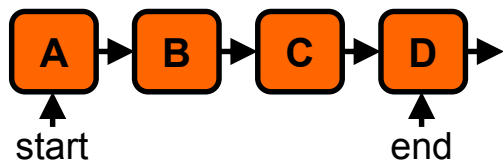
List Implementation: Linked Lists

- Arrays
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 - Need to traverse list to find arbitrary element

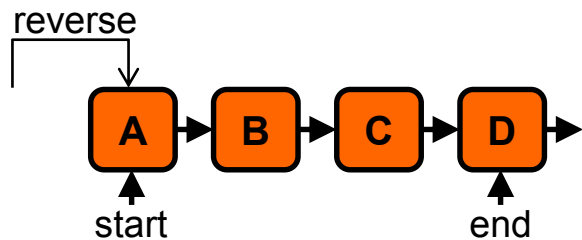
```
public class LinkedList<T> {  
    private class LLNode<T> {  
        T value;  
        LLNode<T> next;  
    }  
    LLNode<T> start;  
    LLNode<T> end;  
}
```



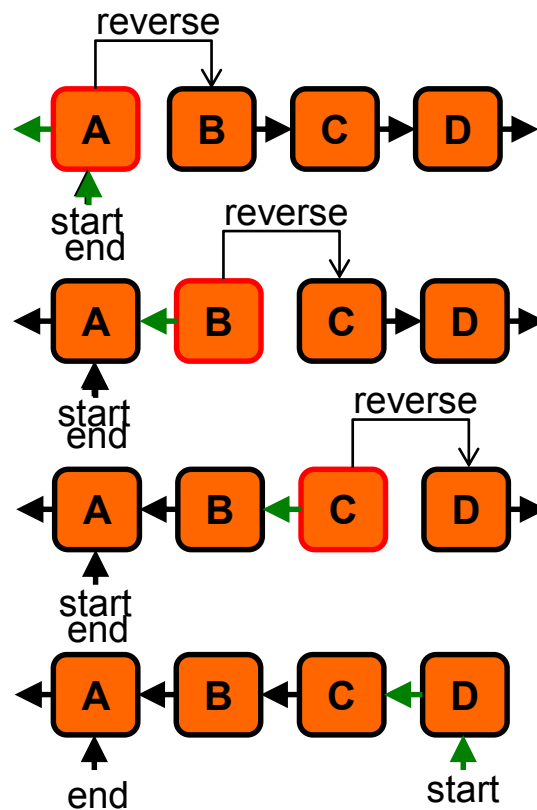
Linked List Reversal



Linked List Reversal



Pointer reversal



Abstract Data Types: Sets



The Set ADT
A Set Interface

The Set ADT

The **set** ADT corresponds to a mathematical *set*. A set has these fundamental properties:

- duplicates *are not* allowed
- order is *not* preserved

A set may support operations such as these:

- *create*: construct an empty set
- *add*: add an element to the set
- *contains*: does the set contain a given element
- *remove*: remove an element from the set

Our Set Interface

We will explore sets using a simple interface :

```
public interface Set<T> {  
    boolean add(T value);  
    boolean contains(T value);  
    int size();  
    boolean remove(T value);  
}
```

Abstract Data Types: Hash Tables

A4

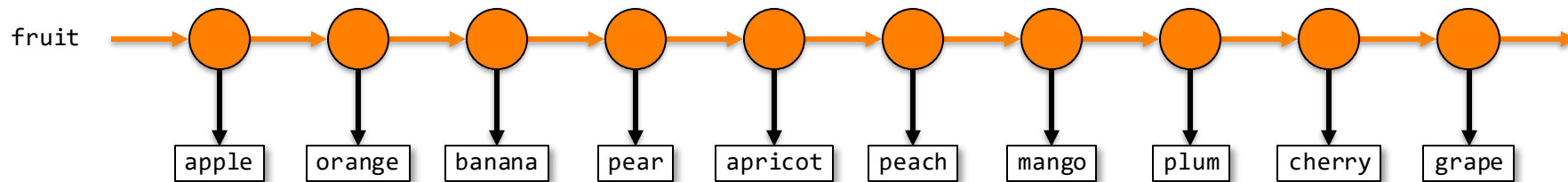
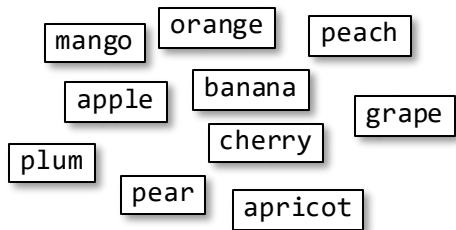
Hash Table
Implementation of a Set 1

Hash Tables

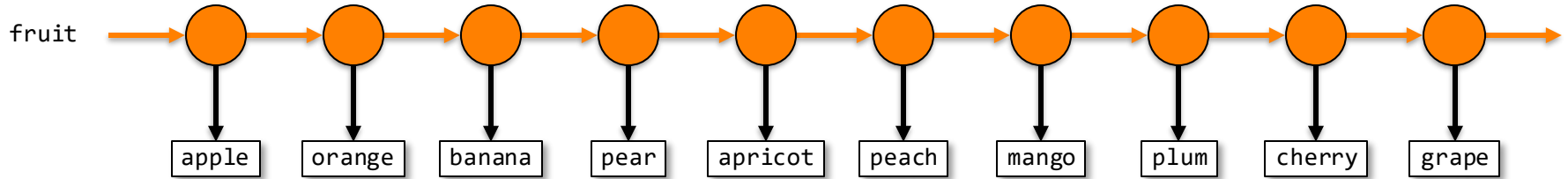
A hash table stores $(key, value)$ pairs, using a hash function to map a key into a table. Key challenges are: a) dealing with hash collisions, and b) dealing with load (how big to make the table).

Two broad approaches:

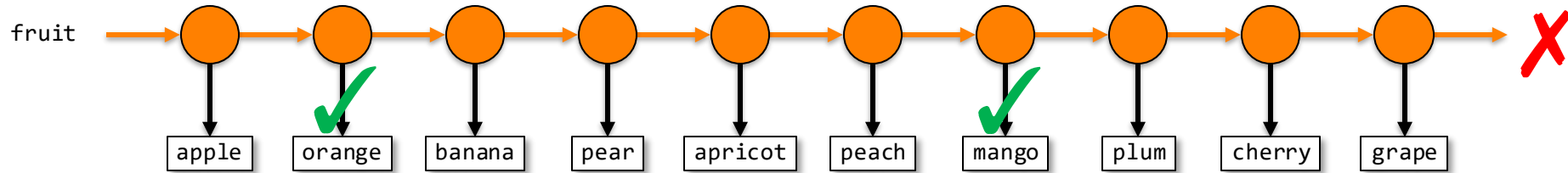
- Separate chaining
 - Hash table entries are lists. $(key, values)$ are in lists.
- Open addressing
 - Hash table entries are $(key, value)$ pairs.
 - Collisions resolved by *probing* – e.g. find next empty slot

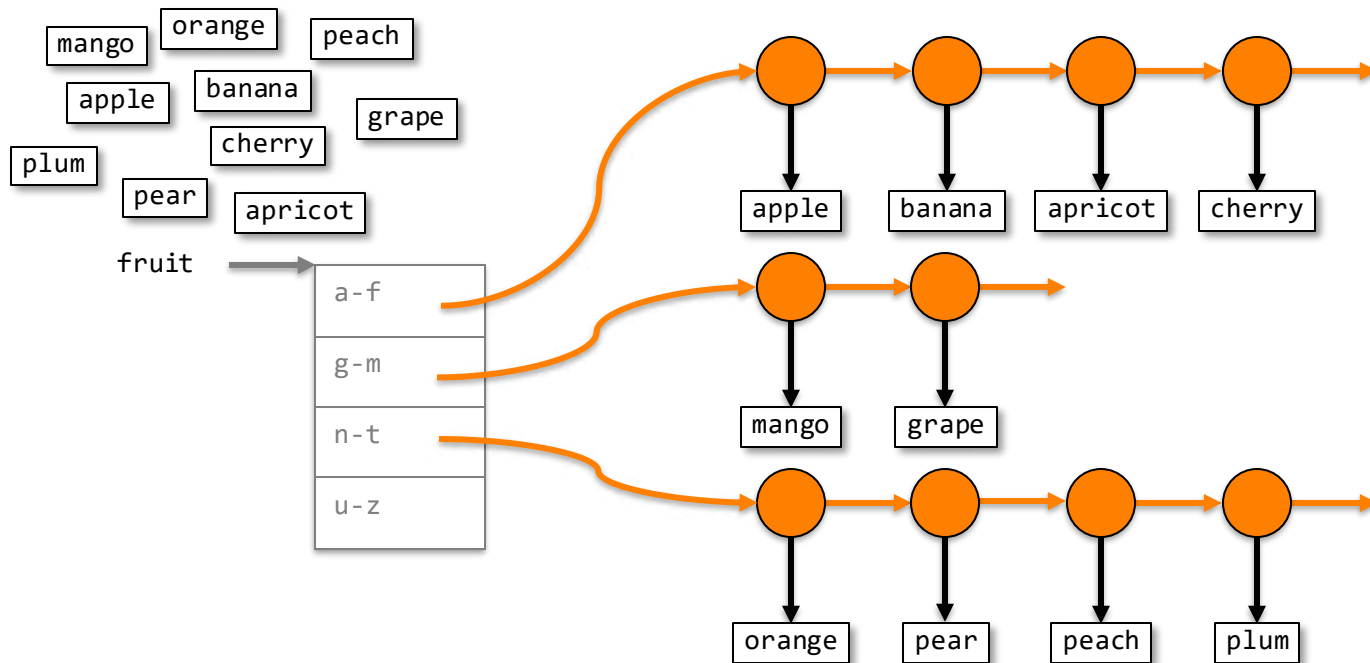


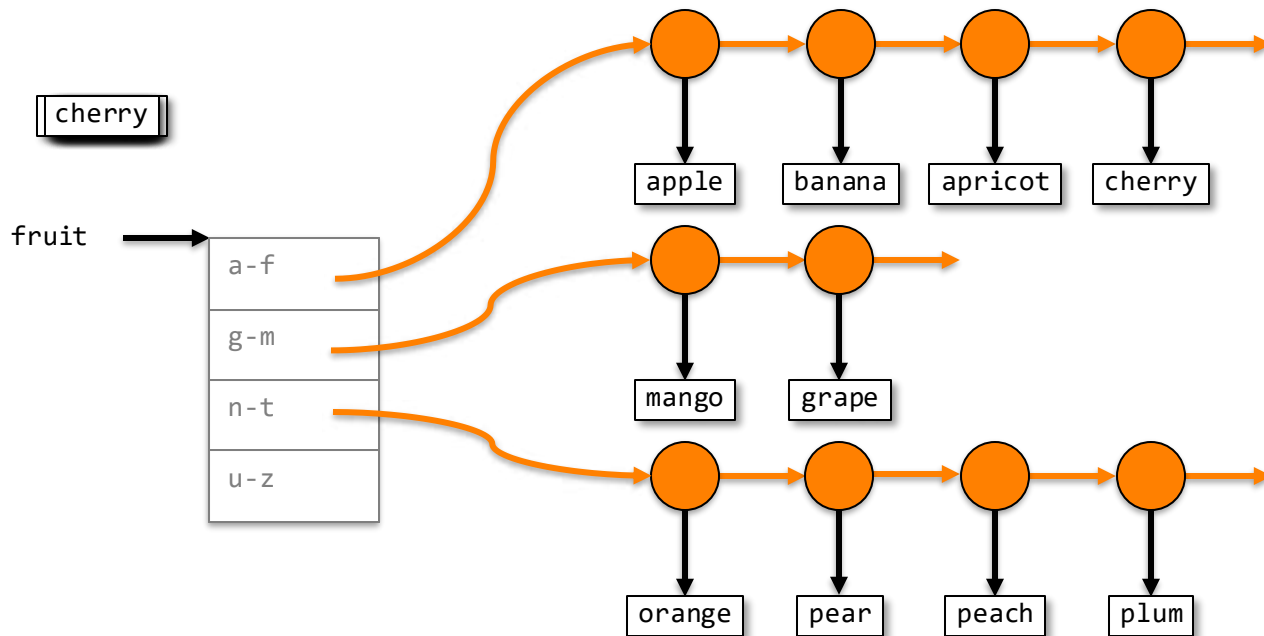

```
fruit.add("apple")
```

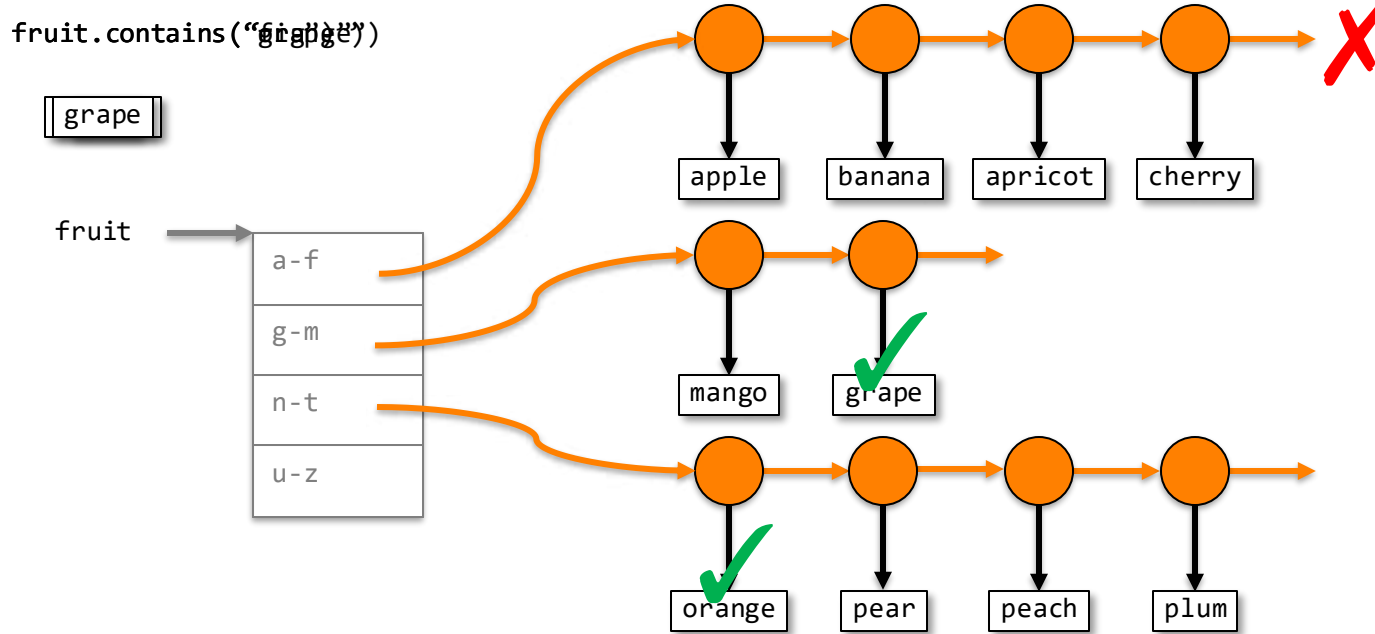


```
fruit.contains("mango")
```









Abstract Data Types: Trees

A5

The Tree ADT
Implementation of a Set 2

The Tree ADT

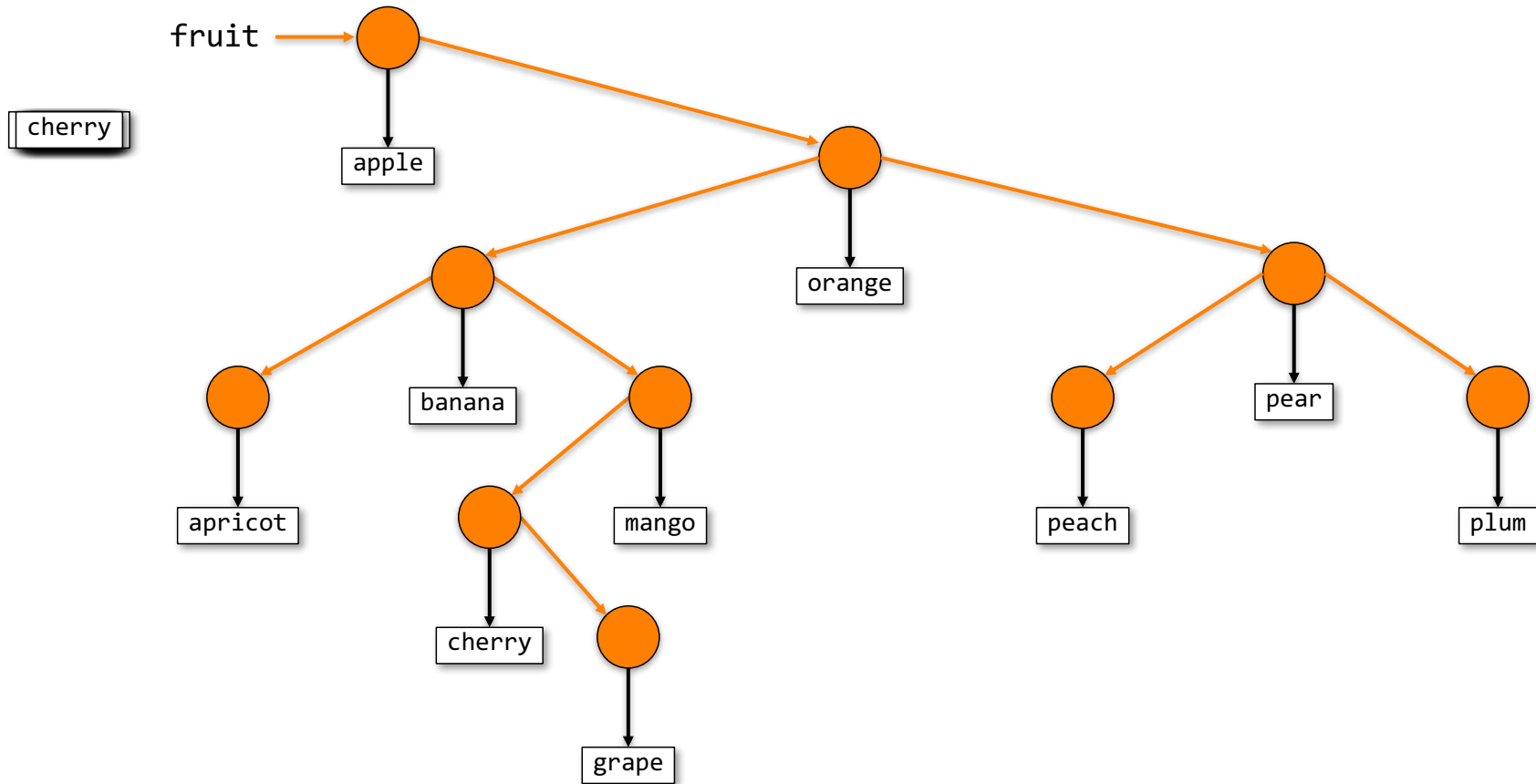
The **tree** ADT corresponds to a mathematical *tree*. A tree is defined recursively in terms of nodes:

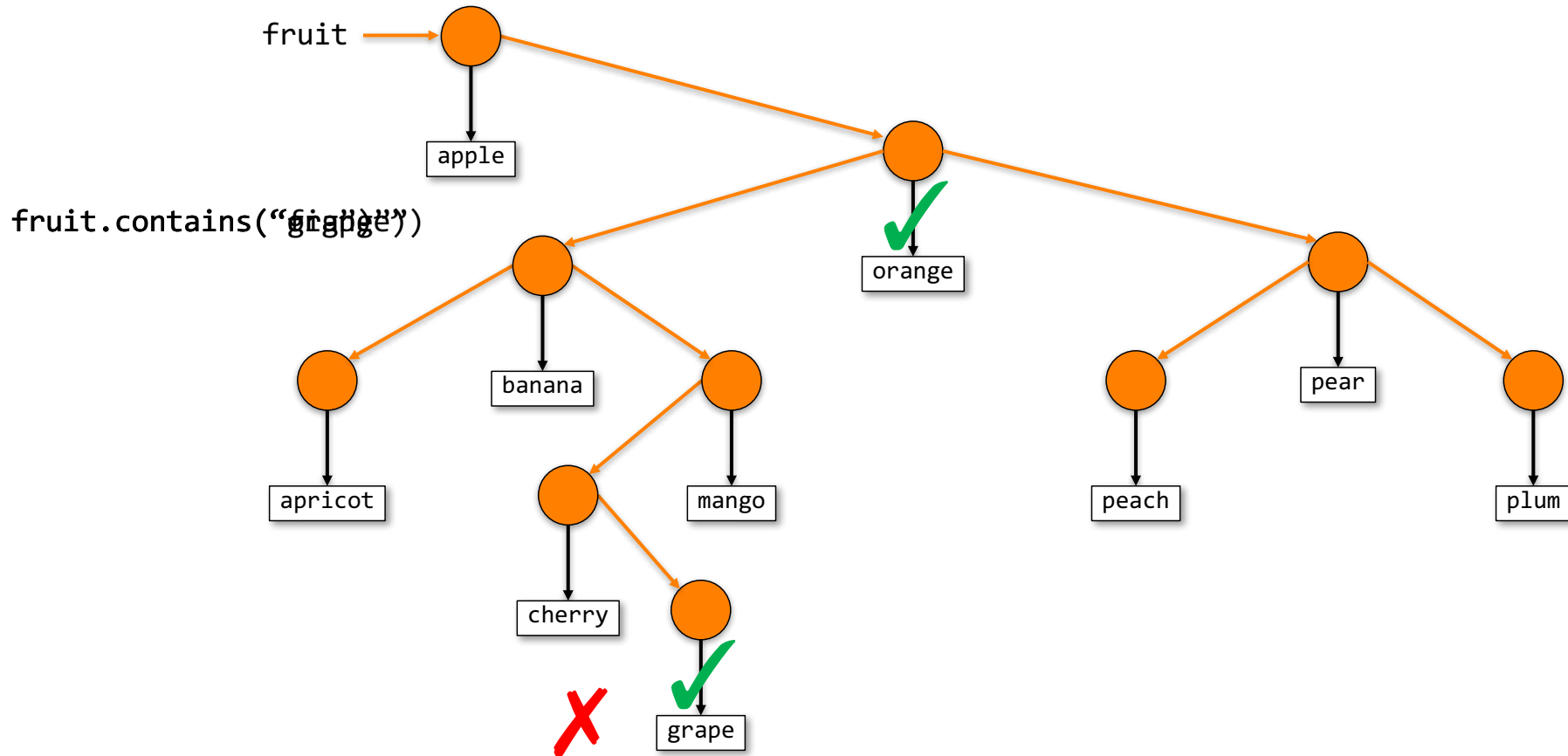
- A tree is a node
- A node contains a *value* and a list of *trees*.
- No node is duplicated.

Binary Search Tree

A **binary** search tree is a tree with the following additional properties:

- Each node has *at most* **two** sub-trees
- Nodes may contain (*key, value*) pairs (or just keys)
- Keys are ordered within the tree:
 - The left sub-tree only contains keys less than the node's key
 - The right sub-tree only contains keys greater than the node's key





Abstract Data Types: Maps

A6

The Map ADT

A Map interface and its implementation

ADT Recap

ADT Recap

First-principles implementation of three Java container types:

- List
 - ArrayList, LinkedList implementations (A1, A2)
- Set
 - HashSet, BSTSet implementations (A3, A4, A5)
- Map
 - HashMap, BSTMap implementations (A6)

Introduced hash tables, trees (A4, A5)

The Map ADT (A.K.A. Associative Array)

A map consists of (key, value) pairs

- Each key may occur only once in the map
- Values are retrieved from the map via the key
- Values may be modified
- Key, value pairs may be removed

Our Map Interface

We will explore maps using a simple interface:

```
public interface Map<K, V> {  
    V put (K key, V value);  
    V get (K key);  
    V remove (K key);  
    int size();  
}
```

fruit.put("orange", 3.50)

grape

fruit

