

A painting of a forest with tall, thin trees and a church spire in the distance. The scene is set in autumn, with yellow and orange leaves on the trees. In the foreground, a person in a blue coat is walking, and another person in a dark coat is standing. The background shows a church spire and a cloudy sky.

A05 Sets: TreeSet

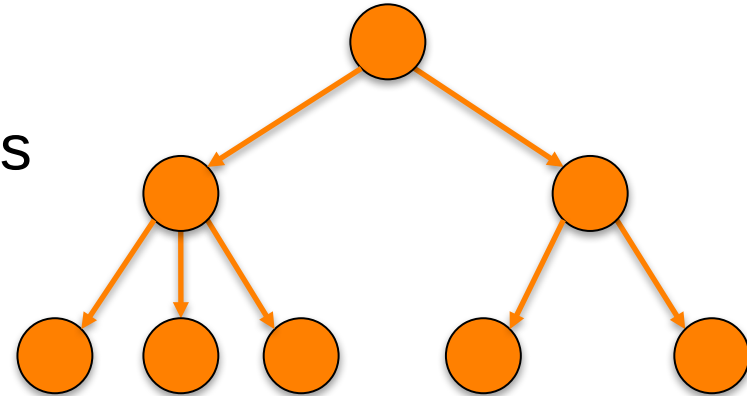
Tree as an ADT
A tree-based Set implementation

Tree as an ADT

The **tree** ADT corresponds to an ordered tree in mathematics.

A tree is defined recursively in terms of nodes:

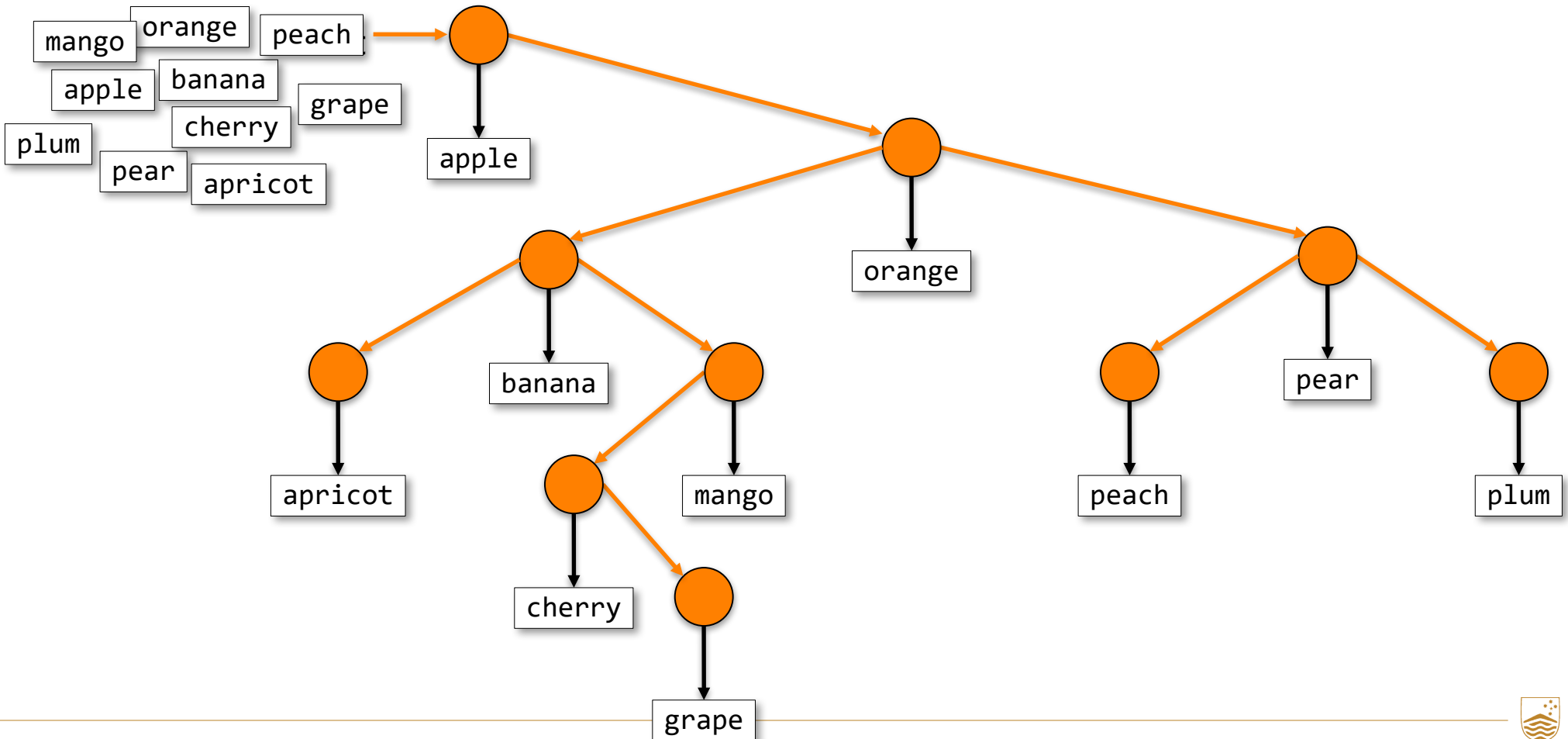
- A tree is a node
- A node contains a value and a list of trees
- No node is duplicated

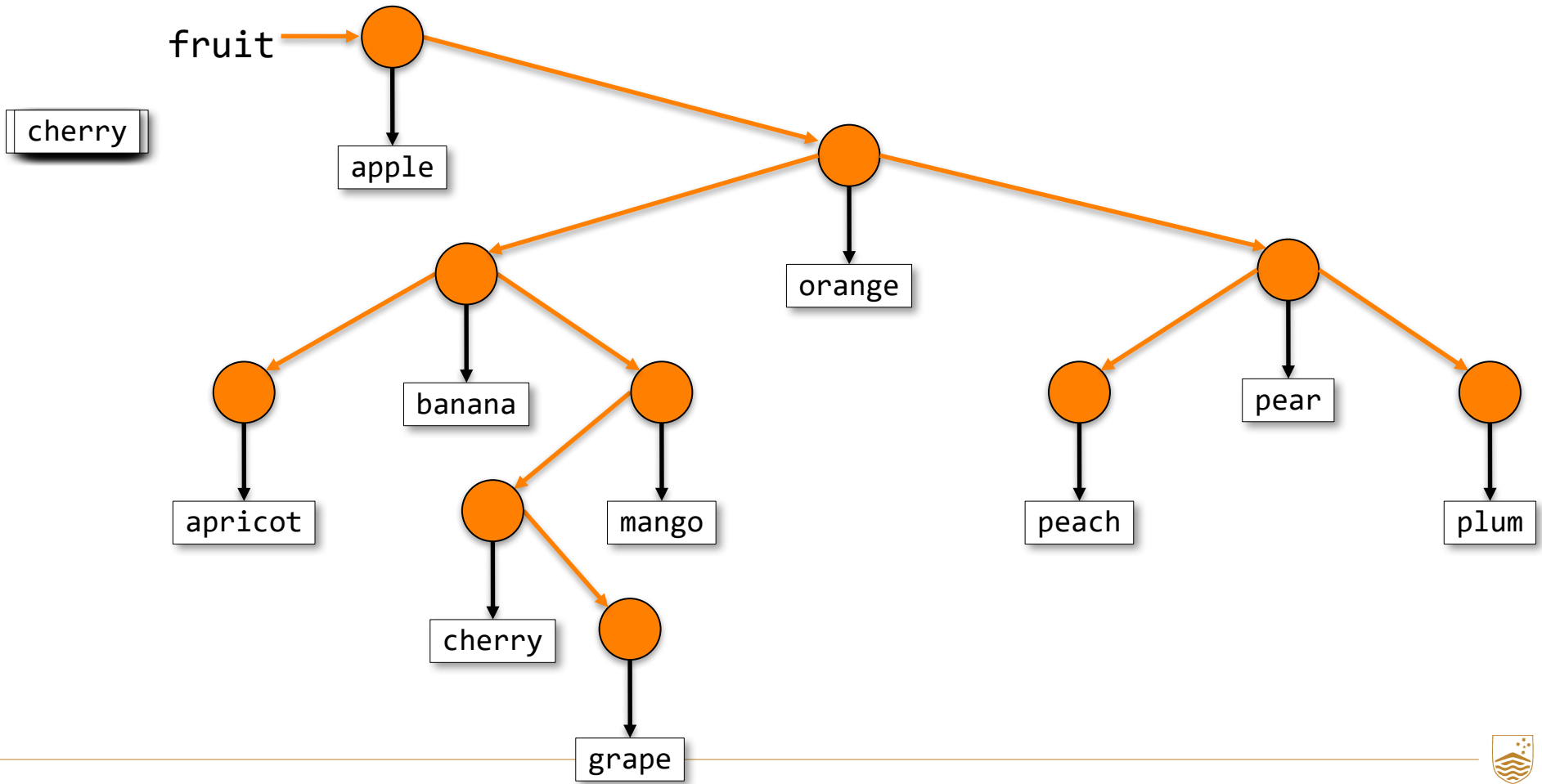


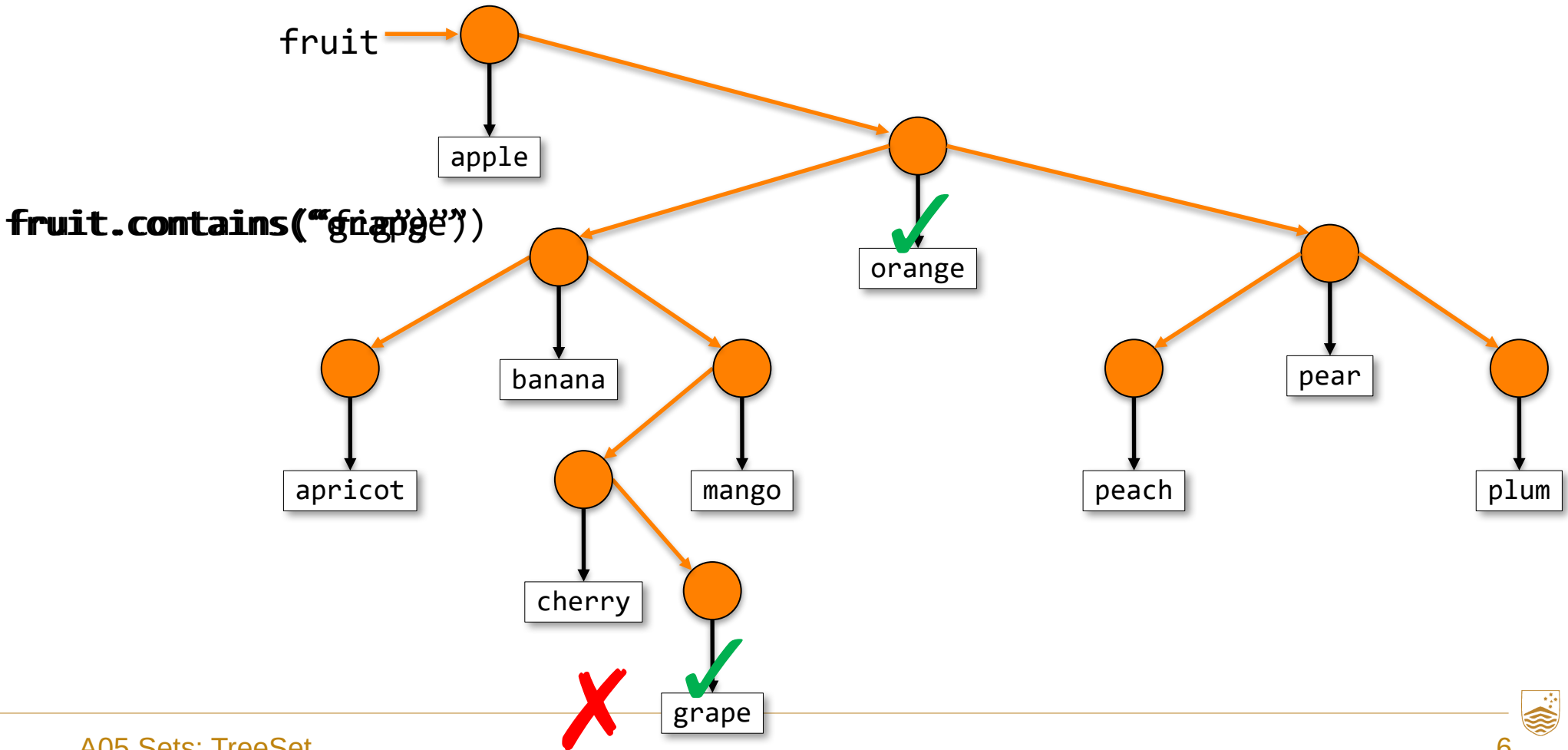
Binary Search Tree to Implement Set

A **binary** search tree is a tree with the following additional properties:

- Each node has at most **two** sub-trees
- Nodes may contain (key, value) pairs, or just keys
- Keys are ordered within the tree:
 - The left sub-tree only contains keys less than the node's key
 - The right sub-tree only contains keys greater than the node's key







Ordering in Java (Recall J14)

Objects of any class that implements the `Comparable` interface can be ordered:

`a.compareTo(b)`

- `< 0` iff a is ordered before b
- `> 0` iff a is ordered after b
- `== 0` if `a.equals(b)` (but also if a and b are not ordered)

Our `Set` interface does not bound our contained type parameter to be `Comparable`, what to do?

- Bound T in the `TreeSet` class declaration:
 - `class TreeSet<T extends Comparable<T>> implements Set<T>`
- Throw runtime exception on use of non-comparable types (the approach in `java.util.TreeSet`).
- Force users to provide `Comparator` (e.g., as lambda expression).

<https://docs.oracle.com/en/java/javase/17/docs/api/java.base/java/lang/Comparable.html>



Complexity

```
boolean add(T value);  
boolean contains(T value);  
int size();  
boolean remove(T value);
```

- add, contains, remove – **Time $O(\log(n))$ amortized, $O(n)$ worst**
 - self-balancing trees (e.g., B-Trees) have $O(\log(n))$ worst case
- size – **Time $O(1)$**
 - explicitly tracked

Space $O(n)$