C03 Graph Traversal

Graphs and Trees Traversal

ANU – School of Computing – Structured Programming 1110 / 1140 / 6710

Graphs and Trees

• A powerful abstraction in computing.



Directed Graph

Nodes: A B C D Edges: (A, B) (B, C) (A, C) (C, A) (A, D)



Directed Rooted Tree

(connected acyclic directed graph)

With ordering of children: Ordered Tree

Tree Features

b is the parent of d and e

d is a **child** of b

b has a **branching factor** (outdegree) of 2 (the number of children)



Traversal

- Visiting the elements in a data structure:
 - searching
 - modifying
 - reachability
 - path finding
- Lists / arrays are a form of "linear data structure" that has a natural sequence for traversal.
- Trees and Graphs can be traversed in many ways.

Tree Traversal

- Special case of graph traversal.
- Two common forms:
 - Depth-First Search (DFS)
 - Explore as deep as possible along a branch until a leaf is reached.
 - *Backtrack* to another branch (e.g., *sibling* of leaf, or sibling of parent, or ...).
 - Breadth-First Search (BFS)
 - Starting at root, visit all nodes at given depth before going deeper.

DFS and BFS



Pre-order DFS traversal **a b d e c f** BFS traversal **a b c d e f**

е

1

b

2

d

4

a

3

6

С

5

C03 Graph Traversal

- 蒙

Implementing Tree Traversal

- Depth-First Search (DFS)
 - Iteratively using a Stack: Last-In First-Out (LIFO) data structure
 - Recursively by implicitly using the *call stack*
 - Variations on ordering: post-order, pre-order, in-order
- Breadth-First Search (BFS)
 - Iteratively using a **Queue**: First-In First-Out (FIFO) data structure
 - *Corecursively** by passing all sub-trees of same level
 - Only one ordering
- * Building (generating) data from a simple "base case", rather than breaking down (reducing) data until base case reached.

Implementation DFS: Stack



Pre-order DFS traversal **a b d e c f** Stack []: *push* onto end, *pop* off end

DFS: pop node, push it's children, repeat.



Implementation BFS: Queue



Queue { }: *enqueue* onto back, *dequeue* off front

BFS: dequeue node, enqueue it's children, repeat.

9



Graph Traversal

- DFS and BFS generalise from tree traversal.
- Starting node selected based on problem.
- Additionally need to **keep track of "visited"** nodes to avoid cycling.



C03 Graph Traversal

Example: Distance Between Nodes

- The *distance* between A and E is the number of edges on a *shortest path* between the two nodes.
- **BFS** can naturally track the distance.
- **DFS** might visit E via a non-shortest *path* need to revisit nodes



C03 Graph Traversal